
Environmental Radioactivity

Physics Laboratory 3

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Abstract Environmental radioactivity was investigated with a focus on ^{222}Rn and its short-lived progeny using three Ranger Radiation Alert detectors. After background measurements, the detectors were calibrated with a 1.9 g KCl sample, yielding consistent calibration factors of about 11–12 Bq/cps.

Radon-related activity was then measured in water and air samples. The water sample showed only a weak excess above background, corresponding to $C_0 = 0.29 \pm 0.13 \text{ Bq L}^{-1}$, so that no reliable half-life could be determined. The air sample gave a clearer signal with $C_0 = 1.14 \pm 0.09 \text{ Bq m}^{-3}$ and an estimated annual dose of $8.60 \pm 0.69 \mu\text{Sv yr}^{-1}$, indicating very low radon exposure in the measured basement environment. Its decay behavior was consistent with the expected order of magnitude of short-lived radon daughters.

An ingrowth measurement on activated carbon showed the buildup of daughter activity toward secular equilibrium, with an effective half-life of $30.74 \pm 0.88 \text{ min}$. Overall, the experiment successfully demonstrated radioactive decay, ingrowth, and secular equilibrium in environmental radioactivity measurements, with the air sample providing the most reliable environmental result.

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1 Introduction

Environmental radioactivity originates mainly from naturally occurring radionuclides present in the Earth's crust, atmosphere, and hydrosphere. Among the most important contributors are ^{40}K and the radionuclides belonging to the primordial decay series of ^{238}U , ^{235}U , and ^{232}Th . These nuclides have existed since the formation of the Earth and continue to decay through long chains of radioactive daughters until stable lead isotopes are reached. As a result, natural radioactivity is a permanent component of the human radiation environment [3].

A particularly important radionuclide in environmental physics and radiochemistry is radon. Radon is a noble gas produced in the decay chains of uranium and thorium, which allows it to escape from soil, rocks, building materials, and water. Because of its gaseous nature, it can migrate through pore spaces and accumulate in enclosed or poorly ventilated areas such as basements, caves, and underground rooms. For this reason, radon is responsible for a large fraction of the average public exposure to ionizing radiation. Among the naturally occurring radon isotopes, ^{222}Rn is the most relevant for environmental measurements because it originates from the ^{238}U decay series and has a comparatively long half-life of 3.8 days.

Although ^{222}Rn itself decays by α emission and could in principle be measured directly with a suitable alpha-detection method, the present experimental setup mainly detects the β -emitting short-lived daughter nuclides, especially ^{214}Pb and ^{214}Bi . These daughter products are therefore well suited for indirect radon measurements with low-level radiation detectors. In addition, the time evolution of parent and daughter nuclides illustrates important concepts of nuclear physics such as radioactive decay, ingrowth, and secular equilibrium. In the case of ^{222}Rn and its progeny, the daughter activity builds up over time and approaches equilibrium with the parent activity after several daughter half-lives.

In this experiment, environmental radioactivity was investigated using a Ranger Radiation Alert detector equipped with a Geiger–Mueller tube. Background radiation was first measured in order to determine the detector baseline. The detector was then calibrated using a potassium chloride sample of known ^{40}K activity. Afterward, radon-related activity was measured in different environmental samples, including air, water, and rock-related samples. Special attention was paid to the ingrowth and decay behavior of radon progeny in order to identify radionuclides from their characteristic half-lives and to study the establishment of secular equilibrium.

The aim of this experiment was to measure environmental radioactivity with a focus on ^{222}Rn and its daughter nuclides, to apply the concepts of radioactive decay and ingrowth to real measurements, and to estimate radon activity in different environmental samples from experimentally observed count rates.

2 Experiment

2.1 Detector and data acquisition

All measurements were performed with a *Ranger Radiation Alert* detector equipped with a Geiger–Mueller tube for low-level radiation measurements. The instrument is capable of detecting α , β , γ , and X-ray radiation, however, under the present experimental conditions it was used mainly as a β detector. In sealed samples, α particles were absorbed by the sample covering, while in air and water measurements the collected activity was dominated by the β -emitting radon progeny, in particular ^{214}Pb and ^{214}Bi . The detector output was recorded in counts per second (cps) using the *Radiation Alert Observer USB* software.

For each measurement, the detector was placed on the sample holder such that the sample faced the detector window without touching it. The Ranger was connected to a computer via USB, and the count rate was logged continuously. The data were saved as plain text files. Only the first two columns, corresponding to time stamp and counts recorded in one second, were used for further analysis.

2.2 Background measurements

Background radiation was measured first in order to determine the detector baseline. For this purpose, the Ranger was placed on an empty sample holder and several measurements of different duration were recorded. Following the recommendation of the manual, measurement times between approximately 10 min and 5 h were used. The purpose of these runs was to compare the statistical fluctuations observed in short and long measurements and to determine a representative background count rate.

The measured background count rate was subtracted from all subsequent measurements, including the detector calibration. Depending on the duration of the measurement, the raw data were rebinned into time intervals of 1 min and 1 h in order to reduce the effect of statistical fluctuations.

2.3 Efficiency calibration

The detector was calibrated using a potassium chloride sample, since natural potassium contains the radioactive isotope ^{40}K . For the calibration, 1.9 g of KCl were ground, weighed, and distributed as homogeneously as possible over an area corresponding approximately to the detector window. The sample was then sealed on both sides with adhesive film in order to avoid contamination of the detector.

The KCl sample was counted for 60 min. A binning interval of 5 min was used for the evaluation. From the known activity A of the calibration sample and the measured net count rate cps_{net} , the calibration factor k was obtained as

$$k = \frac{A}{\text{cps}_{\text{net}}}, \quad (1)$$

where cps_{net} is the background-corrected count rate. The detector efficiency was then defined as

$$\varepsilon = \frac{1}{k}. \quad (2)$$

This calibration factor was later used to convert measured count rates of environmental samples into activity values.

2.4 Measurement of radon in environmental samples

2.4.1 Water sample

Radon activity in water was determined by filtering approximately 2.0 L of water through a fiberglass membrane mounted on a porcelain funnel. After filtration, the membrane was dried on a hotplate for about 5 min and then placed in the sample holder below the detector. Since the expected activity was relatively low and a rapid decay of short-lived radon progeny was anticipated, the sample was measured for less than 5 h and analyzed using binning intervals of 5 min.

2.4.2 Air sample

For the air measurement, approximately 25 m³ of air should be pumped through a glass fiber filter using a dust-collecting pump. The initial and final pumped volumes were recorded to determine the total sampled air volume. However, the total sampled air volume was determined to be only 3.96 m³, the meter scale had initially been misread. To maximize radon collection, air was preferentially sampled in a poorly ventilated indoor environment, the basement of the HPP building on the ETH Honggerberg campus. After sampling, the filter was placed in the sample holder and measured for about 10 h. Depending on the count rate evolution, binning times of 10 min were used.

The measured count rates from both water and air samples were converted into activities using the calibration factor determined from the KCl measurement.

2.5 Ingrowth and decay of radon progeny

The ingrowth and decay behavior of radon daughters was studied using activated carbon exposed to radon emanating from radioactive source materials. The purpose of this part of the experiment was to observe the buildup and decay of the short-lived progeny of ²²²Rn and to identify characteristic half-lives from the measured activity curves.

For the ingrowth measurement, activated carbon was placed in a glass beaker and attached to adhesive film. The activated carbon was then rapidly exposed to the sample container such that the carbon faced the source and adsorbed emanated radon for 5 min. After exposure, the carbon was sealed with a second adhesive film and placed in the sample holder. The activity was measured for approximately 5 h, and the data were rebinned into intervals of 5 or 10 min. The resulting ingrowth curve was later fitted to extract the characteristic buildup of the daughter activity.

For the decay measurement, the same procedure was used, but the activated carbon was exposed to the radon source for a longer period of 2 h in order to collect a larger amount of ^{222}Rn . The sealed sample was then measured over about three days, using a binning interval of 1 h. Because the software is known to show a gradual increase in the time interval between recorded rows during very long measurements, the multi-day decay data were expected to be more reliable for a qualitative than for a fully quantitative half-life determination.

2.6 Data treatment

The raw detector output consisted of one-second count data stored in text format. Because radioactive decay is inherently stochastic, the count rate fluctuated strongly on short time scales. To reduce statistical scatter, the one-second data were grouped into fixed time bins. For each bin, the total number of counts was first calculated,

$$N_{\text{bin}} = \sum_i n_i,$$

with Poisson uncertainty

$$\sigma_{N_{\text{bin}}} = \sqrt{N_{\text{bin}}}.$$

The binned count rate was then obtained as

$$\text{cps}_{\text{bin}} = \frac{N_{\text{bin}}}{\Delta t}.$$

Thus, each bin was treated as one independent measurement point of the decay or ingrowth curve.

Different bin widths were used depending on the measurement type and the expected rate of change of the activity. Shorter bin widths were chosen for rapidly varying samples, such as water and air filters, whereas longer bin widths were applied to slowly varying measurements such as the multi-day decay runs. For all samples, the background count rate was subtracted before further analysis. Activity values were then obtained by multiplying the net count rate by the calibration factor k .

3 Results & Discussion

3.1 Background measurements

Before evaluating the calibration and environmental sample measurements, the background count rate of each detector was analyzed. According to the manual, the relevant information is contained in the first two columns of the raw text files, namely the time stamp and the number of detected counts in one second. Since the raw one-second count rate fluctuates strongly because of the random nature of radioactive decay, the data were additionally binned over longer time intervals in order to obtain a more stable representation of the background behavior.

For detector 1, two background measurements of different duration were available: a short measurement of 10 minutes and a longer measurement of 5 hours. For detectors 2 and 3, background measurements of 2 hours and 3 hours, respectively, were analyzed. The 10-minute run of detector 1 was binned into 1-minute intervals, whereas the longer runs were binned into 1-hour intervals. For each measurement, the total counting time, the mean count rate, its Poisson uncertainty, the standard deviation of the raw one-second counts, and the standard deviation of the binned count rates were determined.

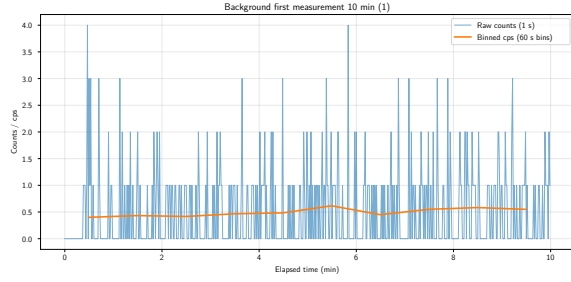
Table 1: Summary of the analyzed background measurements. The quoted uncertainty of the mean count rate was obtained from Poisson counting statistics.

Measurement	Time (min)	Bin size (s)	Mean cps	σ_{mean}	σ_{binned}
Detector 1	10	60	0.495	0.029	0.075
Detector 1	300	3600	0.503	0.005	0.015
Detector 2	120	3600	0.540	0.009	0.011
Detector 3	180	3600	0.539	0.007	0.020

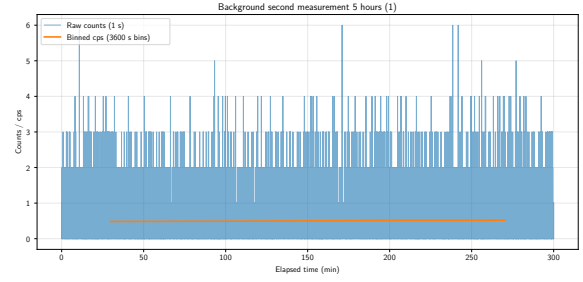
The corresponding background curves are shown in Fig. 1. For all three detectors, the background behavior is stable over the full measurement interval, and the mean count rates are mutually consistent. Detector 2 and detector 3 yield nearly identical mean background values, both close to 0.54 cps, while detector 1 gives 0.495 ± 0.029 cps for the 10-minute run and 0.503 ± 0.005 cps for the 5-hour run. The agreement between the two measurements of detector 1 shows that the detector background is reproducible and of the same order of magnitude as for the other two detectors.

As expected, the short 10-minute background run of detector 1 is more strongly affected by statistical fluctuations than the longer measurements. This is reflected in its larger uncertainty of the mean count rate, σ_{mean} , as well as in the larger spread of the binned values, σ_{binned} . Such behavior is consistent with Poisson counting statistics, since a shorter acquisition time provides fewer total counts and therefore leads to larger relative fluctuations. In contrast, the longer background measurements yield smoother binned curves and smaller statistical uncertainties. Overall, the background analysis confirms that all

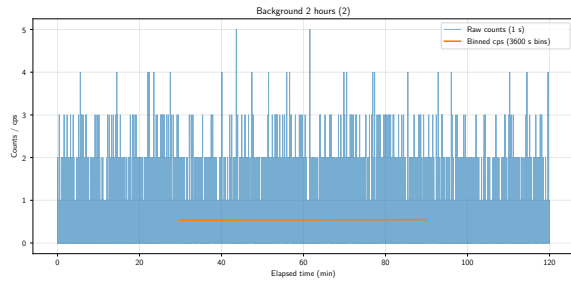
detectors provide stable and consistent baseline count rates, which were subsequently used for the background correction of the KCl calibration measurements.



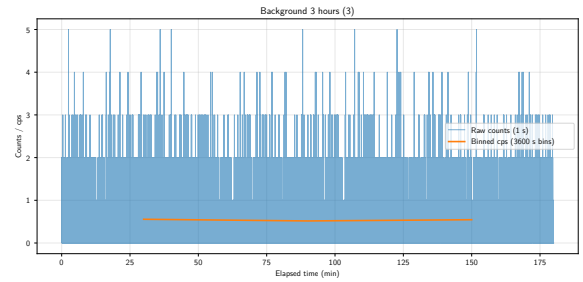
(a) Detector 1, first background measurement (10 min, 60 s bins).



(b) Detector 1, second background measurement (5 h, 3600 s bins).



(c) Detector 2 background measurement (2 h, 3600 s bins).



(d) Detector 3 background measurement (3 h, 3600 s bins).

Figure 1: Background measurements for the three Ranger detectors. The blue curves show the raw one-second counts, while the orange curves represent the binned count rates over longer time intervals. All three detectors exhibit stable and consistent background levels. As expected, the short 10-minute run of detector 1 is more affected by statistical fluctuations than the longer measurements.

Regarding the reduction and control of the measured background, several practical improvements can be suggested. To improve the determination of the detector background, longer and repeated background measurements should be preferred, since they reduce the relative statistical uncertainty and make transient fluctuations easier to identify. Moreover, the detector should be kept in a stable environment and as far as possible from radioactive samples, contaminated surfaces, or temporarily elevated radon concentrations. A constant detector position and unchanged measurement geometry are also important in order to avoid artificial variations between runs. If available, additional shielding or measurements in a location with lower environmental radiation could further reduce the background level and improve the sensitivity for weak samples.

3.2 Calibration efficiency

The activity of the KCl calibration sample was calculated from the abundance of the radioactive isotope ^{40}K in natural potassium. Since each KCl molecule contains one potassium atom, the number of potassium atoms in the sample is obtained from the sample mass and the molar mass of KCl. Multiplying this by the natural isotopic abundance of

^{40}K yields the number of radioactive atoms,

$$N_{^{40}\text{K}} = \frac{m_{\text{KCl}}}{M_{\text{KCl}}} N_A f_{^{40}\text{K}}. \quad (3)$$

The activity then follows from

$$A_{^{40}\text{K}} = \lambda N_{^{40}\text{K}}, \quad \lambda = \frac{\ln 2}{T_{1/2}}, \quad (4)$$

where $T_{1/2}$ is the half-life of ^{40}K , not of KCl itself. Using $m_{\text{KCl}} = 1.9 \text{ g}$, $M_{\text{KCl}} = 74.5513 \text{ g/mol}$ [2], $f_{^{40}\text{K}} = 0.000117$, and $T_{1/2}(^{40}\text{K}) = (1.248 \pm 0.003) \times 10^9 \text{ y}$ [1], the theoretical activity of ^{40}K in the calibration sample is found to be

$$A_{^{40}\text{K}} = 31.60 \text{ Bq}. \quad (5)$$

For each detector, the KCl calibration measurement was performed over 1 h, and the recorded count-rate data were additionally binned into 5 min intervals. The net count rate was then obtained by subtracting the detector-specific background count rate,

$$\text{cps}_{\text{net}} = \text{cps}_{\text{raw}} - \text{cps}_{\text{bg}}. \quad (6)$$

From the net count rate, the calibration factor was calculated as

$$k = \frac{A_{^{40}\text{K}}}{\text{cps}_{\text{net}}}, \quad (7)$$

and the detector efficiency was determined from

$$\varepsilon = \frac{1}{k}. \quad (8)$$

As a consistency check, detector 1 was calibrated using two different background assignments: first with the short 10 min background measurement, and second with the long 5 h background measurement. The resulting calibration plots are shown in Fig. 2, and the numerical results are summarized in Table 2.

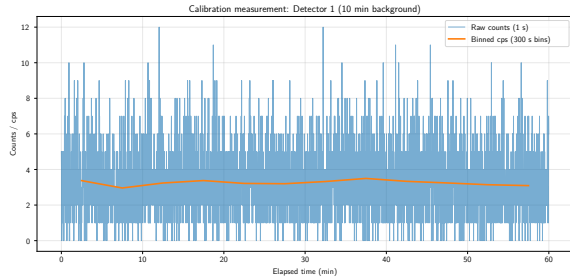
Table 2: Calibration results for the three Ranger detectors. For detector 1, two background assignments were evaluated using the 10 min and 5 h background measurements, respectively. Both cases yield consistent calibration results within uncertainty.

Detector	cps_{bg} (s^{-1})	cps_{raw} (s^{-1})	cps_{net} (s^{-1})	k (Bq/cps)	ε (cps/Bq)
1a	0.495 ± 0.029	3.250 ± 0.030	2.755 ± 0.042	11.47 ± 0.17	0.0872 ± 0.0013
1b	0.503 ± 0.005	3.250 ± 0.030	2.747 ± 0.031	11.50 ± 0.13	0.0869 ± 0.0010
2	0.540 ± 0.009	3.360 ± 0.031	2.820 ± 0.032	11.21 ± 0.13	0.0892 ± 0.0010
3	0.539 ± 0.007	3.182 ± 0.030	2.643 ± 0.031	11.96 ± 0.14	0.0836 ± 0.0010

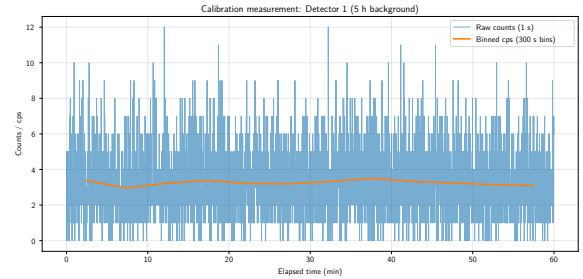
The calibration results of detectors 2 and 3 are mutually consistent. Both detectors yield similar background-subtracted count rates and therefore similar calibration factors and efficiencies. Detector 1 now shows the same overall behavior. Using either the 10 min or the 5 h background measurement, the resulting net count rates remain clearly positive and lead to calibration factors and efficiencies that are in very good agreement with those of detectors 2 and 3. The two background assignments for detector 1 give $k = 11.47 \pm 0.17 \text{ Bq/cps}$ and $k = 11.50 \pm 0.13 \text{ Bq/cps}$, respectively, showing that the calibration result is stable with respect to the choice of background measurement.

As expected, the use of the longer 5 h background measurement for detector 1 leads to a smaller uncertainty than the 10 min background case, because the background count rate is determined more precisely from the larger number of recorded counts. Nevertheless, both detector 1 calibrations are fully consistent within uncertainty and also agree well with the corresponding values obtained for detectors 2 and 3. Overall, all three Ranger detectors exhibit comparable efficiencies, with calibration factors in the range of about 11–12 Bq/cps and efficiencies close to 0.09 cps/Bq.

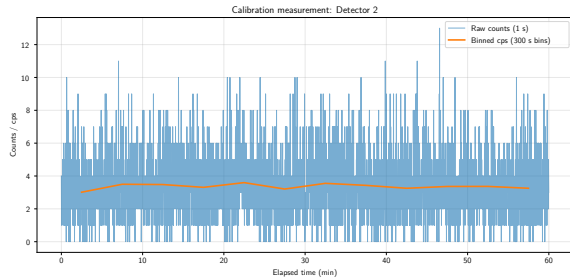
For the following evaluation, the calibration based on the 5 h background measurement is adopted for detector 1, since it provides the smaller statistical uncertainty. The 10 min background case is retained as a consistency check and confirms that the detector response is reproducible within the expected counting statistics.



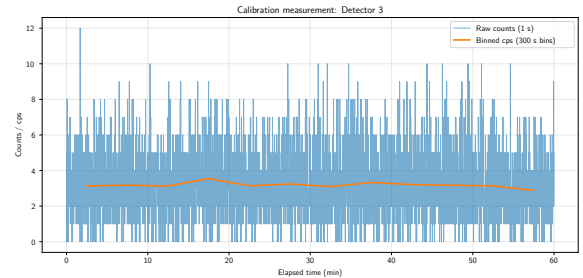
(a) Detector 1 using the 10 min background.



(b) Detector 1 using the 5 h background.



(c) Detector 2 calibration measurement.



(d) Detector 3 calibration measurement.

Figure 2: Calibration measurements of the three Ranger detectors using the 1.9 g KCl reference sample. The blue curves show the raw one-second counts, while the orange curves represent the count rate binned in 300 s intervals. Two background assignments were evaluated for detector 1, using the 10 min and 5 h background measurements, respectively. All four cases, including both background assignments for detector 1, yield consistent background-corrected count rates and calibration results within uncertainty.

In the present experiment, no separate calibration factor for ^{222}Rn was determined independently. Instead, the manual instructs using the detector calibration factor obtained from the KCl efficiency calibration to convert the measured count rates into radon-related activity. Thus, for the subsequent ^{222}Rn analysis, the effective k factor is taken to be the same detector-specific calibration factor determined from the KCl reference measurement. This gives $k = 11.50 \pm 0.13 \text{ Bq/cps}$ for detector 1, $k = 11.21 \pm 0.13 \text{ Bq/cps}$ for detector 2, and $k = 11.96 \pm 0.14 \text{ Bq/cps}$ for detector 3. For detector 1, the calibration obtained with the 10 min background measurement is fully consistent within uncertainty and therefore confirms the robustness of the adopted value.

3.3 Measurement of Rn in Environmental Samples

3.3.1 Water sample

The background-corrected activity curve of the water sample, obtained from approximately 2.0 L of filtered water, is shown in Fig. 3. After conversion with the detector-specific calibration factor of detector 2, only a weak net signal is obtained. The fitted initial activity is

$$A_0 = 0.58 \pm 0.27 \text{ Bq},$$

which corresponds to an initial radon concentration of

$$C_0 = 0.29 \pm 0.13 \text{ Bq L}^{-1}.$$

Thus, the water sample exhibits only a small excess above background, and the statistical uncertainties remain comparatively large over the full measurement interval.

A single-exponential fit to the decay curve yields an apparent half-life of

$$T_{1/2} = 190 \pm 390 \text{ min.}$$

However, this result is not meaningful from a physical point of view, since the uncertainty is larger than the central value itself. In addition, the fitted half-life is not compatible with the literature values of the short-lived radon progeny responsible for the detected β activity, namely ^{214}Pb with $T_{1/2} = 26.9 \text{ min}$ and ^{214}Bi with $T_{1/2} = 19.7 \text{ min}$ [3]. The water measurement is therefore best interpreted as a low-activity sample for which a rough concentration estimate can still be obtained, whereas a reliable half-life determination is not possible.

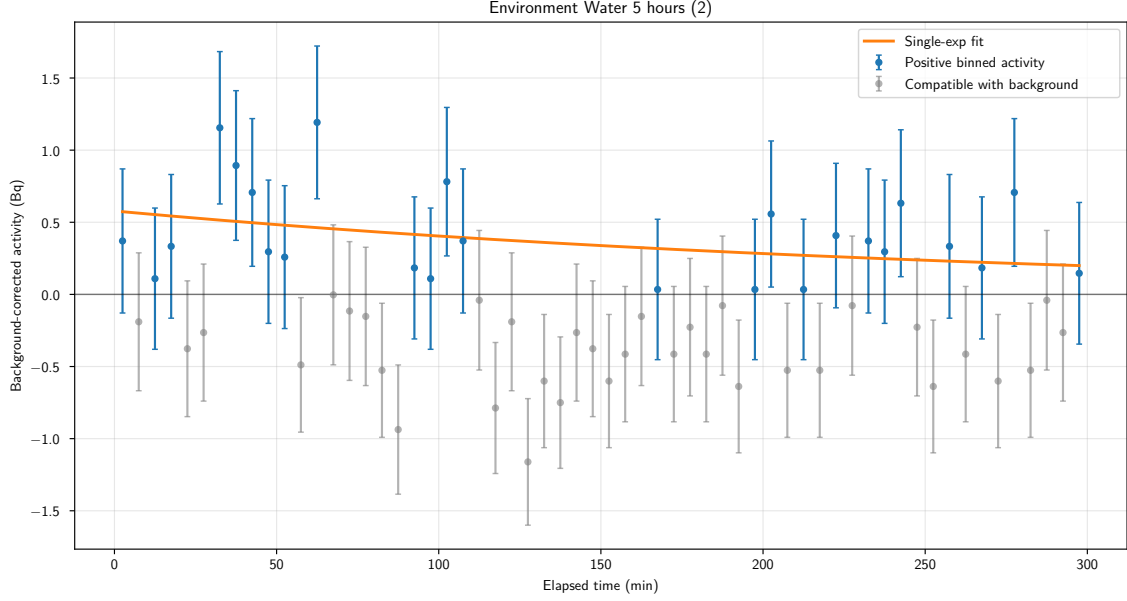


Figure 3: Background-corrected activity of the water sample measured with detector 2 as a function of elapsed time. The data were binned in 300 s intervals and converted into activity using the calibration factor determined from the ^{40}K activity in the KCl calibration sample. Blue points indicate positive background-corrected activity values, whereas gray points are bins compatible with background after subtraction and were not used for the exponential fit. Because the net signal is weak and strongly affected by statistical fluctuations, the extracted half-life should be interpreted with caution.

3.3.2 Air sample

The activity curve obtained from the air filter sample is shown in Fig. 4. In contrast to the water measurement, the air sample exhibits a clear decay immediately after the start of the measurement. From the gas meter readings before and after sampling, the total sampled air volume was determined to be only 3.96 m^3 , the meter scale had initially been misread. Using the calibration factor of detector 3, the fitted initial activity is

$$A_0 = 4.52 \pm 0.37 \text{ Bq},$$

which corresponds to an initial radon concentration of

$$C_0 = 1.14 \pm 0.09 \text{ Bq m}^{-3}.$$

To estimate the corresponding annual dose, the relation given in the laboratory manual was used,

$$D = C_0 (\varepsilon_r + \varepsilon_d F) O, \quad (9)$$

where C_0 is the radon activity concentration in Bq m^{-3} , $\varepsilon_r = 0.17 \text{ nSv h}^{-1} (\text{Bq m}^{-3})^{-1}$ is the dose conversion factor for radon itself, $\varepsilon_d = 9 \text{ nSv h}^{-1} (\text{Bq m}^{-3})^{-1}$ is the dose conversion factor for the short-lived progeny, F is the equilibrium factor between radon and its daughters, and O is the indoor occupancy time. Following the manual, $F = 0.4$ was

used. For the occupancy factor, a conventional workplace value of $O = 2000 \text{ h yr}^{-1}$ was assumed, consistent with UNSCEAR practice for indoor workplaces [4]. This yields an annual dose estimate of

$$D = (8.60 \pm 0.69) \mu\text{Sv yr}^{-1}.$$

This dose is very small. Likewise, the measured radon concentration is low compared with typical indoor radon concentrations reported in the literature. According to the WHO, outdoor radon concentrations are usually of the order of 5 to 15 Bq m^{-3} , whereas indoor concentrations commonly start at about 10 Bq m^{-3} and may reach well above 100 Bq m^{-3} , depending on ventilation and local geology [7]. The value measured in the ETH basement is therefore lower than typical indoor concentrations and even below the usual outdoor range.

This suggests that the HPP basement is not strongly radon contaminated. However, the result should be interpreted with caution. The sampled air volume was smaller than originally intended, and the filter method detects mainly the short-lived radon progeny rather than gaseous ^{222}Rn directly. The obtained concentration should therefore be regarded as an approximate lower estimate rather than a precise absolute radon concentration for the basement.

The decay behavior of the air-filter activity was analyzed using two different models. First, a single-exponential fit was applied in order to describe the data by one effective decay component only. The corresponding model is

$$A(t) = A_0 e^{-\lambda t},$$

where A_0 is the initial activity and λ is the decay constant. The associated half-life is then given by

$$T_{1/2} = \frac{\ln 2}{\lambda}.$$

This model provides an effective half-life for the overall decay of the collected radon progeny.

Applying this fit to the measured air-sample activity yields

$$T_{1/2} = (43.6 \pm 4.6) \text{ min}.$$

This value is somewhat larger than the literature half-lives of the dominant short-lived radon daughters, namely ^{214}Pb with $T_{1/2} = 26.9 \text{ min}$ and ^{214}Bi with $T_{1/2} = 19.7 \text{ min}$, but it is still of the same order of magnitude. Since the measured count rate originates from the combined contribution of radon progeny collected on the filter, such an effective half-life is physically plausible.

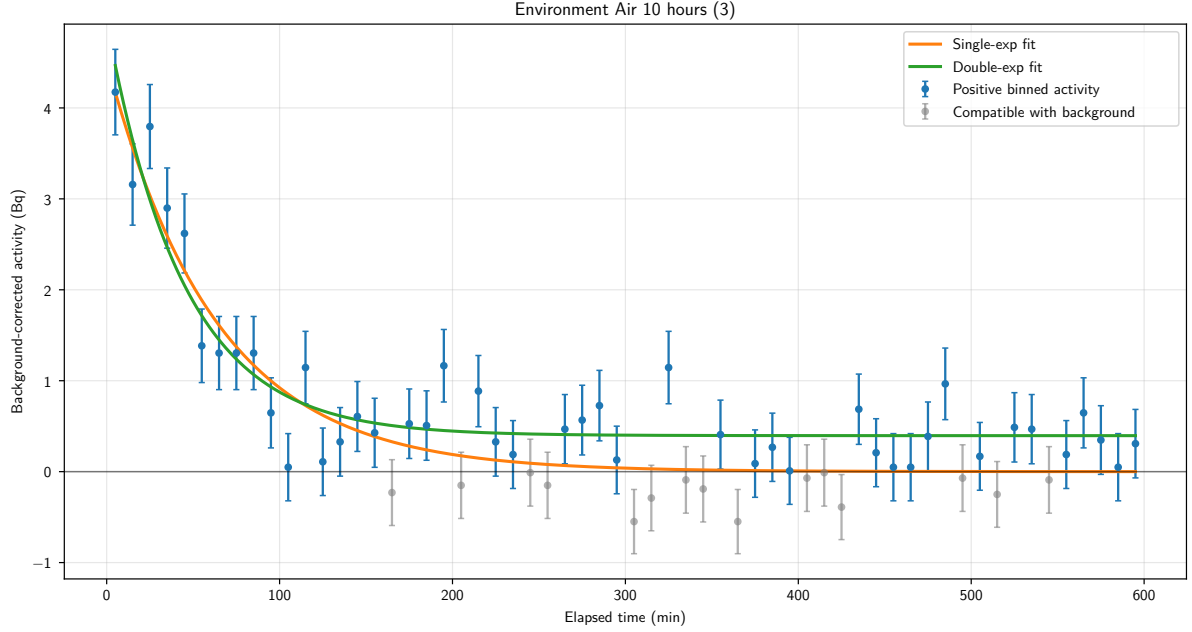


Figure 4: Background-corrected activity of the air filter sample measured with detector 3 as a function of elapsed time. The data were binned in 600s intervals and converted into activity using the ^{40}K calibration factor. Blue points indicate positive background-corrected activity values, whereas gray points are bins compatible with background after subtraction and were not used for the exponential fits. Both a single-exponential and a double-exponential fit are shown. The rapid initial decrease is clearly visible, whereas the late-time data approach the background level.

To test whether more than one decay component contributes to the measured activity, the data were also fitted with a double-exponential model of the form

$$A(t) = A_1 e^{-\lambda_1 t} + A_2 e^{-\lambda_2 t},$$

where A_1 and A_2 are the amplitudes of the two components and λ_1 , λ_2 are their respective decay constants. The corresponding half-lives are

$$T_{1/2,1} = \frac{\ln 2}{\lambda_1}, \quad T_{1/2,2} = \frac{\ln 2}{\lambda_2}.$$

This more flexible model was used to check whether the decay curve contains more than one characteristic slope, as expected if different short-lived daughter isotopes contribute with different relative weights.

For this purpose, the air data were additionally displayed on a logarithmic scale and fitted with the double-exponential model, as shown in Fig. 5. The fast component yields

$$T_{1/2,\text{fast}} = (30.8 \pm 9.8) \text{ min},$$

which is reasonably consistent with the expected decay of the short-lived ^{222}Rn daughters, mainly ^{214}Pb and ^{214}Bi , within uncertainty. The slow component yields a much longer half-life. In principle, such a component could indicate contributions from other radon

decay chains, for example from ^{220}Rn in the thorium series through its daughter ^{212}Pb , or from later daughters in the ^{222}Rn decay chain. However, the slow component is not well constrained by the present data and appears mainly at late times, where the activity is close to the background level. Therefore, it should not be interpreted as a reliable identification of an additional isotope.

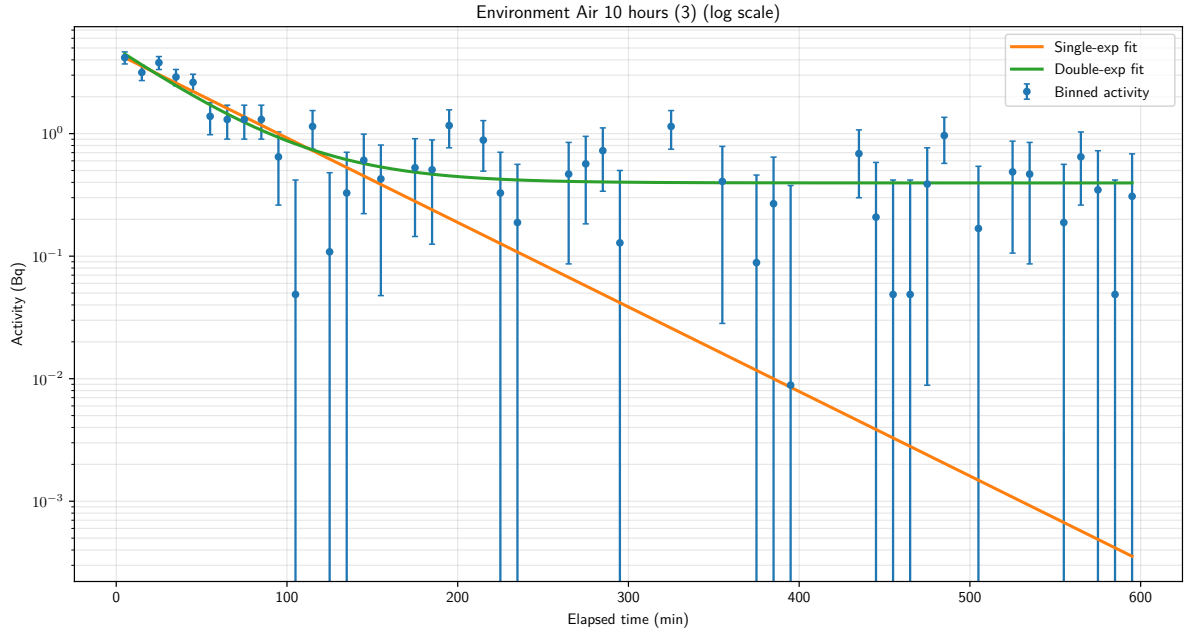


Figure 5: Same air-sample activity data as in Fig. 4, but shown on a logarithmic scale. The logarithmic representation highlights the approximately exponential initial decay and shows that the second, very slow component of the double-exponential fit is not physically meaningful.

Overall, the air sample provides the more reliable environmental radon result. Compared with the water sample, it shows a much clearer excess above background and allows at least an approximate identification of the relevant short-lived radon progeny through the observed decay behavior.

For additional perspective, the estimated annual dose from the air sample,

$$D = 8.60 \pm 0.69 \mu\text{Sv yr}^{-1},$$

is extremely small compared with other common sources of radiation exposure. According to the US EPA, consuming one banana corresponds to a dose of about $0.1 \mu\text{Sv}$ due to naturally occurring ^{40}K [5]. The dose estimated for the HPP basement air sample is therefore comparable to the dose from about 86 bananas per year. At the same time, it is negligible compared with the average annual radiation dose to the public, which the US NRC gives as about 6.2 mSv yr^{-1} in the United States [6]. This comparison further supports the conclusion that the measured radon-related dose in the investigated HPP basement is very low.

3.4 Ingrowth and Decay of ^{222}Rn and its Progeny

This part of the experiment was designed to study both the buildup of the short-lived radon daughters after a short exposure to emanated radon and the subsequent long-time decay behavior after a longer adsorption period on activated carbon. The ingrowth measurement was recorded over about 4 h and evaluated with a binning interval of 300 s, while the long decay measurement extended over about 72 h and was evaluated with 3600 s bins.

3.4.1 Ingrowth

The ingrowth curve is shown in Fig. 6. As expected, the measured activity rises rapidly at early times and then gradually approaches a constant saturation level, indicating that secular equilibrium between ^{222}Rn and its short-lived progeny is being established.

To describe this behavior, the Bateman equations for a parent–daughter decay chain were used in their simplified form. Since the half-life of ^{222}Rn is much longer than the duration of the ingrowth measurement, the parent activity can be treated as approximately constant over the observed time interval. In this limit, the daughter activity follows

$$A(t) = A_{\infty} (1 - e^{-\lambda t}),$$

where A_{∞} is the equilibrium activity and λ is the effective decay constant of the daughter activity. The corresponding half-life is given by

$$T_{1/2} = \frac{\ln 2}{\lambda}.$$

The fit yields an equilibrium activity of

$$A_{\infty} = (37.76 \pm 0.32) \text{ Bq}$$

and an effective half-life of

$$T_{1/2} = (30.74 \pm 0.88) \text{ min.}$$

This value is of the same order of magnitude as the literature half-lives of the dominant short-lived radon daughters, in particular ^{214}Pb with $T_{1/2} = 26.9 \text{ min}$ and ^{214}Bi with $T_{1/2} = 19.7 \text{ min}$. Since the detected β -activity originates from the combined contribution of these daughter nuclides, such an effective half-life is physically plausible.

Using the fitted half-life, seven daughter half-lives correspond to

$$7 T_{1/2} = (3.59 \pm 0.10) \text{ h.}$$

Equivalently, the fitted ingrowth model gives a time of

$$t_{99\%} = (3.40 \pm 0.10) \text{ h}$$

to reach 99% of the equilibrium activity. In addition, after seven half-lives the fractional approach to equilibrium is

$$1 - 2^{-7} = 0.9922,$$

that is, about 99.2%. This demonstrates quantitatively that secular equilibrium between ^{222}Rn and ^{214}Pb is effectively reached after about seven ^{214}Pb half-lives, in agreement with the expectation from the Bateman equations.

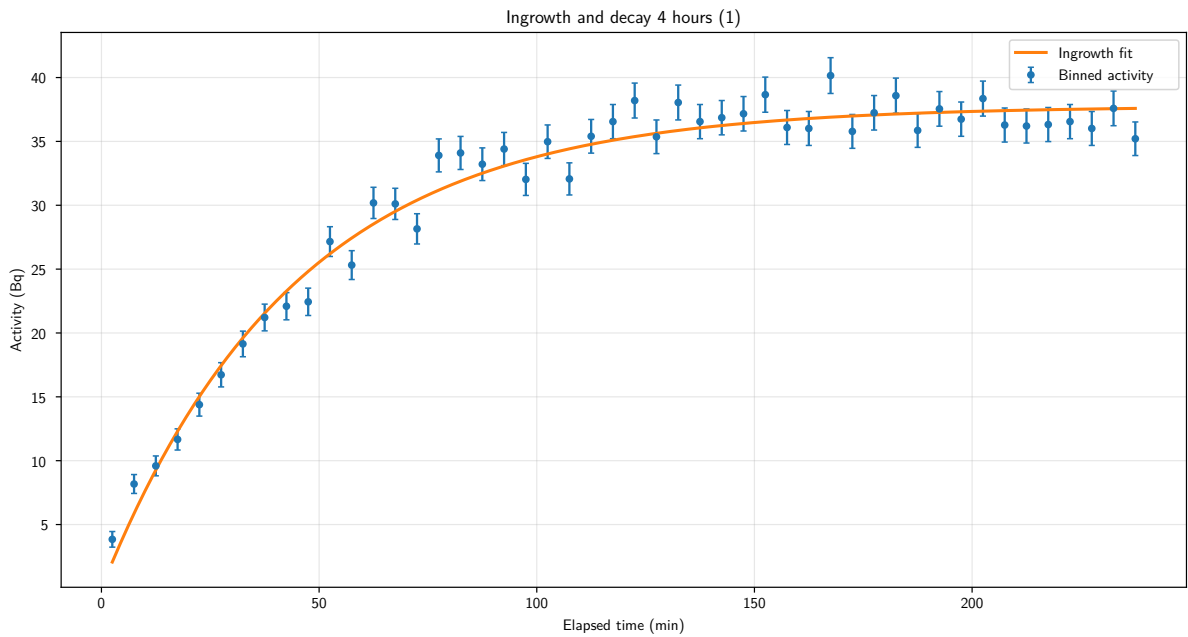


Figure 6: Background-corrected activity of the ingrowth measurement as a function of elapsed time. The data were binned in 300s intervals and fitted with an ingrowth model approaching a saturation activity A_∞ . The curve shows the gradual establishment of secular equilibrium between ^{222}Rn and its short-lived progeny.

3.4.2 Long decay measurement

The long decay measurement is shown in Fig. 7. Immediately after the start of the measurement, the activity decreases rapidly, whereas at later times the data approach a nearly constant residual level. A single-exponential model,

$$A(t) = A_0 e^{-\lambda t},$$

was fitted to the decay data, giving

$$A_0 = 136.89 \pm 1.51 \text{ Bq}$$

and

$$T_{1/2} = 1.339 \pm 0.010 \text{ h.}$$

This fitted half-life is far smaller than the literature half-life of ^{222}Rn ,

$$T_{1/2}(^{222}\text{Rn}) = 91.76 \text{ h,}$$

and therefore cannot be interpreted as the true decay constant of ^{222}Rn . Instead, the measured decay is dominated by the activity of short-lived daughter nuclides at early times. In the ^{222}Rn decay chain, ^{218}Po has a very short half-life of about 3.1 min and therefore decays rapidly to ^{214}Pb without significant accumulation on the time scale of the measurement. The observed β activity is thus mainly governed by ^{214}Pb and ^{214}Bi , while later daughters such as ^{210}Pb or ^{210}Bi could only contribute to a slow residual component because of their much longer half-lives. Contributions from other radon decay chains, for example, ^{220}Rn from the thorium series, cannot be fully excluded either. The fitted value should therefore be regarded as an effective half-life of a mixed daughter activity rather than a direct measurement of the ^{222}Rn half-life.

The logarithmic representation in Fig. 8 further shows that the late-time data deviate strongly from a pure single-exponential decay and remain close to a residual background-like level. This confirms that the long measurement is not well described by a single decay component over the full 72 h interval.

Consequently, the long decay run should be interpreted mainly qualitatively. It clearly demonstrates the rapid loss of daughter activity after the sample has been removed from the radon source, but it does not provide a reliable experimental determination of the true ^{222}Rn half-life. This is consistent with the known limitation of long measurements in the manual, namely that the effective time spacing between recorded rows may drift over long acquisition times.

Under the simplifying assumptions of secular equilibrium between ^{226}Ra and its daughters before sampling and 100% adsorption efficiency of ^{222}Rn on the activated carbon, the measured initial activity can be used to estimate the activity of ^{226}Ra in the uranium rock. Using the 2 h adsorption time, this gives

$$A(^{226}\text{Ra}) = (9.13 \pm 0.10) \times 10^3 \text{ Bq.}$$

This value should be regarded only as a rough order-of-magnitude estimate, since it depends directly on the strong assumptions of ideal secular equilibrium and complete ^{222}Rn adsorption on the activated carbon. In reality, the adsorption efficiency may be smaller than 100%, and part of the radon may not be trapped or may desorb again during the measurement. In addition, small leaks in the adhesive-film sealing could allow some radon to escape from the sample. Such effects would reduce the measured activity and could also

make the observed decay appear faster than expected. Therefore, the calculated ^{226}Ra activity should not be interpreted as a precise quantitative value.

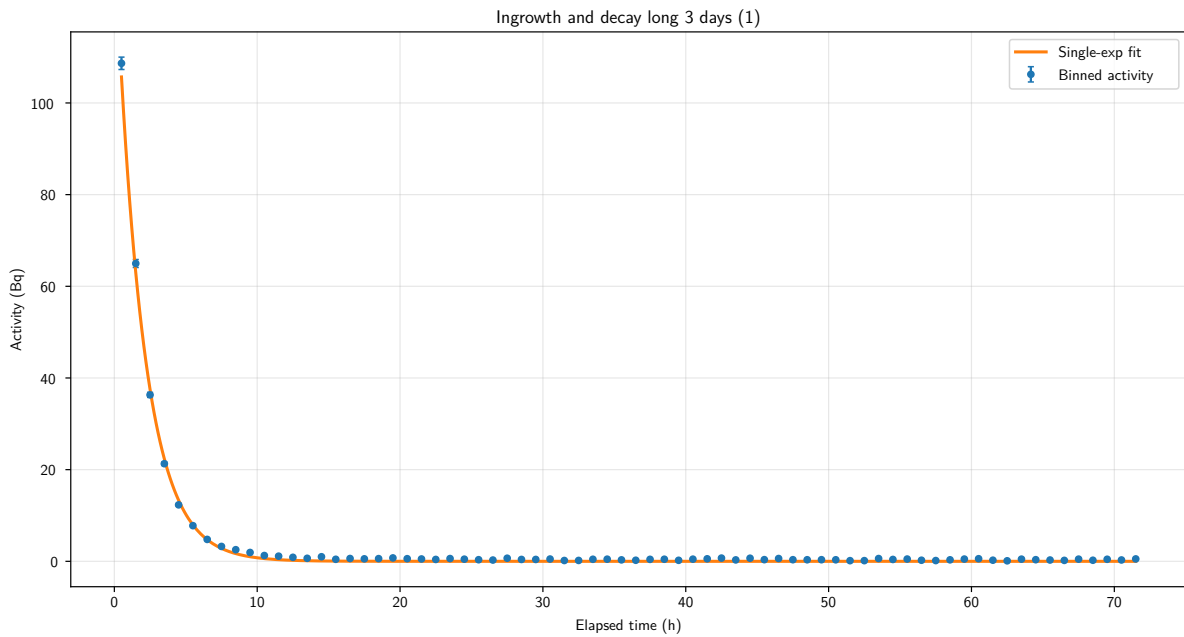


Figure 7: Background-corrected activity of the long decay measurement as a function of elapsed time. The data were binned in 3600s intervals and fitted with a single-exponential decay model. The rapid initial decrease is visible on the linear scale, but the late-time behavior is not well described by a pure exponential.

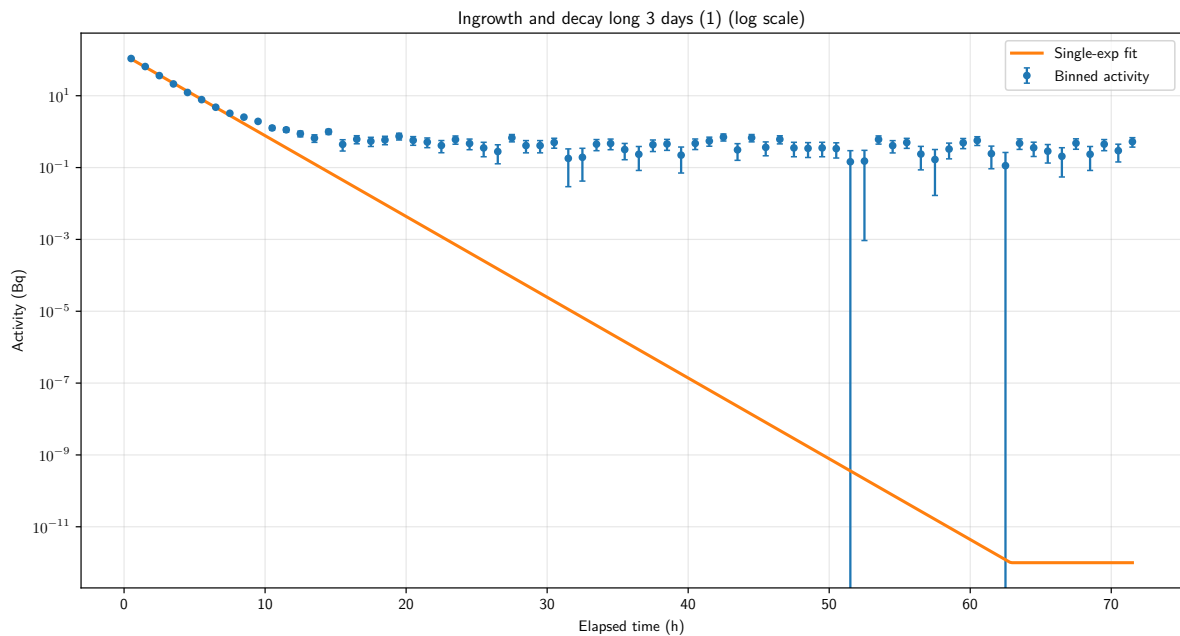


Figure 8: Same long decay data as in Fig. 7, but shown on a logarithmic scale. The logarithmic representation highlights the clear deviation from a pure single-exponential decay at late times, where the activity approaches a residual background-like level.

4 Conclusion

In this experiment, environmental radioactivity was investigated with a focus on ^{222}Rn and its short-lived progeny. The background measurements showed that all three Ranger detectors provided stable and mutually consistent baseline count rates. As expected from Poisson statistics, the shorter background run exhibited larger relative fluctuations, while the longer measurements yielded smaller uncertainties. The subsequent efficiency calibration with the KCl reference sample also gave consistent results for all detectors, with calibration factors in the range of about 11–12 Bq/cps and efficiencies close to 0.09 cps/Bq. This confirms that the detector response was reproducible and that the KCl calibration was suitable for the conversion of measured count rates into radon-related activity.

For the environmental samples, the water measurement showed only a weak excess above background. The fitted initial activity was $A_0 = 0.58 \pm 0.27 \text{ Bq}$, corresponding to a radon concentration of $C_0 = 0.29 \pm 0.13 \text{ Bq L}^{-1}$. Because of the low signal and the large statistical fluctuations, the fitted half-life was not physically meaningful, so the water sample mainly allows a rough concentration estimate. In contrast, the air filter sample yielded a much clearer signal. The initial activity was found to be $A_0 = 4.52 \pm 0.37 \text{ Bq}$, corresponding to $C_0 = 1.14 \pm 0.09 \text{ Bq m}^{-3}$, and the associated annual dose estimate was $D = 8.60 \pm 0.69 \mu\text{Sv yr}^{-1}$. This value is very small, indicating that the investigated HPP basement was not strongly radon contaminated. The decay analysis of the air sample gave an effective half-life of $T_{1/2} = 43.6 \pm 4.6 \text{ min}$ for the single-exponential model, while the fast component of the double-exponential fit yielded $T_{1/2,\text{fast}} = 30.8 \pm 9.8 \text{ min}$. Both values are of the expected order of magnitude for the short-lived radon daughters and therefore support their identification as the dominant contributors to the measured β activity.

The ingrowth measurement further demonstrated the establishment of secular equilibrium between ^{222}Rn and its short-lived progeny. The fitted equilibrium activity was $A_\infty = 37.76 \pm 0.32 \text{ Bq}$ and the effective half-life was $T_{1/2} = 30.74 \pm 0.88 \text{ min}$, which is consistent with the expected behavior of the combined daughter activity. The analysis showed that about 99% of equilibrium is reached after approximately $3.40 \pm 0.10 \text{ h}$, in agreement with the Bateman-based expectation of about seven daughter half-lives. By contrast, the long decay measurement could only be interpreted qualitatively. Although it clearly showed the rapid loss of daughter activity after removal from the radon source, the fitted half-life of $1.339 \pm 0.010 \text{ h}$ is far below the literature half-life of ^{222}Rn and therefore does not represent the true radon decay. The estimated ^{226}Ra activity of the uranium rock, $A(^{226}\text{Ra}) = (9.13 \pm 0.10) \times 10^3 \text{ Bq}$, should therefore only be regarded as an order-of-magnitude estimate because it depends on strong simplifying assumptions, in particular ideal secular equilibrium, complete radon adsorption on the activated carbon, and the absence of leakage or desorption.

Overall, the experiment successfully illustrated the main concepts of environmental radioactivity, radioactive decay, ingrowth, and secular equilibrium using real measurements. The most reliable environmental result was obtained from the air sample, whereas the water measurement was limited by low activity and poor counting statistics. The main limitations of the experiment were the weak signal strength of some samples, the smaller-than-intended sampled air volume, and the limited reliability of very long measurements. Nevertheless, the results are physically consistent and show that the Ranger detector, together with a simple KCl calibration, is well suited for the qualitative and semi-quantitative investigation of environmental radon and its progeny.

Appendix

Acknowledgments

I would like to thank my lab partner, Denis Seibel, for the good collaboration throughout this experiment. We carried out the measurements together and jointly collected the data used in this report.

I would like to thank my teaching assistant, Dr. Miriam Mindová, for her supervision and support during the experiment. Her guidance and explanations were very helpful throughout the laboratory work and the interpretation of the results.

AI Usage Declaration

This report was prepared with assistance from ChatGPT (OpenAI) for language polishing, formatting suggestions, and for helping to develop, debug, and correct the syntax of the Python code. The AI was not used to generate raw data, to select results, or to determine the final conclusions. All scientific content (methods, calculations, results, and interpretation) was critically reviewed and validated by the authors. The authors take full responsibility for the accuracy of the analysis and for any remaining errors. No confidential or personal data were provided to the AI system during the preparation of this report.

Safety Measures

Several safety precautions were followed throughout the experiment in order to minimize unnecessary radiation exposure and to avoid contamination of the detector and the working area. Since the main radionuclides investigated in this experiment were ^{222}Rn and its short-lived progeny, particular care was taken when handling samples that had been exposed to radon emanation.

The detector window of the Ranger instrument was treated as a sensitive component and was never touched either by the sample or by the operator. During all measurements, the samples were placed in the holder in such a way that no direct contact with the detector window occurred. In addition, the activated carbon and KCl samples were sealed with adhesive film before being placed under the detector in order to prevent contamination.

To reduce inhalation exposure, measurements involving airborne radon progeny were carried out in a controlled way and the sampled filters were handled only for the time required to transfer them into the sample holder. The activated carbon exposed to radon was sealed immediately after sampling. More generally, unnecessary proximity to radioactive samples was avoided, and the samples were returned to their designated storage location after the measurements.

Finally, standard laboratory safety rules were respected throughout the experiment. In particular, the workplace was kept organized, the measurement setup was handled carefully, and all experimental procedures were performed according to the instructions given in the laboratory manual and by the teaching assistant.

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Python Code

1. Background Measurement.py

```
1 from pathlib import Path
2 import re
3 from datetime import datetime
4 import math
5
6 import numpy as np
7 import pandas as pd
8 import matplotlib.pyplot as plt
9
10
11
12 # =====
13 # PATHS
14 # =====
15
16 # Assumed location:
17 # Datenauswertung/
18 # Python Code/
19 #     BackgroundAnalysis.py
20 # Messdaten/
21
22 BASE_DIR = Path(__file__).resolve().parent.parent
23 DATA_DIR = BASE_DIR / "Messdaten"
24 OUTPUT_DIR = BASE_DIR / "background_analysis_output"
25 OUTPUT_DIR.mkdir(exist_ok=True)
26
27
28 # =====
29 # USER SETTINGS
30 # =====
31
32 # Here you define which background folders you want to analyze
33 # and which bin size (in seconds) should be used for each one.
34 #
35 # Suggested examples:
36 # 60 s    = 1 min
37 # 300 s   = 5 min
38 # 600 s   = 10 min
```

```

39 # 1800 s = 30 min
40 # 3600 s = 1 hour
41
42 BACKGROUND_CONFIG = {
43     "Background first measurement 10 min (1)": 60,
44     "Background second measurement 5 hours (1)": 3600,
45     "Background 2 hours (2)": 3600,
46     "Background 3 hours (3)": 3600,
47 }
48
49 # If you want to also save the binned data as csv files:
50 SAVE_BINNED_DATA = True
51
52 # If you want plots to pop up interactively:
53 SHOW_PLOTS = True
54
55
56 # =====
57 # HELPERS
58 # =====
59
60 def extract_device_number(folder_name: str):
61     match = re.search(r"((\d+)\)\s*$", folder_name)
62     return int(match.group(1)) if match else None
63
64
65 def extract_datetime_from_filename(filename: str):
66     """
67     Example:
68     Chart 2026_03_30 13.04.44.txt
69     """
70     match = re.search(r"(\d{4}_\d{2}_\d{2})\s+(\d{2}\.\d{2}\.\d{2})", filename)
71     if not match:
72         return None
73     return datetime.strptime(
74         f"{match.group(1)} {match.group(2)}",
75         "%Y_%m_%d %H.%M.%S"
76     )
77
78
79 def list_txt_files_sorted(folder: Path):

```

```

80     files = list(folder.glob("*.txt"))
81     return sorted(files, key=lambda f: extract_datetime_from_filename(f.name)
82                   or datetime.min)
83
84 def normalize_name(name: str):
85     return name.strip().lower()
86
87
88 def find_folder_by_exact_name(folder_name: str):
89     for folder in DATA_DIR.iterdir():
90         if folder.is_dir() and normalize_name(folder.name) ==
91            normalize_name(folder_name):
92             return folder
93         raise FileNotFoundError(f"Folder not found: {folder_name}")
94
95 # =====
96 # TXT READING
97 # =====
98
99 def read_measurement_file(file_path: Path):
100     """
101     Read only the first two columns:
102     1) Date/Time
103     2) counts (1 sec)
104
105     Ignore all columns from column 3 onward, exactly as stated in the manual.
106     """
107     encodings = ["utf-8", "latin1", "cp1252"]
108     last_error = None
109
110     for enc in encodings:
111         try:
112             df = pd.read_csv(
113                 file_path,
114                 sep="\t",
115                 encoding=enc,
116                 usecols=[0, 1]
117             )
118             break

```

```

119     except Exception as e:
120         last_error = e
121     else:
122         raise RuntimeError(f"Could not read {file_path.name}: {last_error}")
123
124     df.columns = ["Date/Time", "counts"]
125
126     out = pd.DataFrame()
127     out["datetime"] = pd.to_datetime(
128         df["Date/Time"],
129         format="%Y.%m.%d %H:%M:%S",
130         errors="coerce"
131     )
132     out["counts"] = pd.to_numeric(df["counts"], errors="coerce")
133     out["source_file"] = file_path.name
134     out["file_start_datetime"] = extract_datetime_from_filename(file_path.name)
135
136     out = out.dropna(subset=["counts"]).copy()
137     out["counts"] = out["counts"].astype(float)
138
139     return out
140
141
142 def read_folder_measurement(folder: Path):
143     """
144     Read all txt files in chronological order and concatenate them.
145     Each row corresponds to one second of measurement.
146     """
147     txt_files = list_txt_files_sorted(folder)
148     if not txt_files:
149         raise FileNotFoundError(f"No txt files found in folder: {folder.name}")
150
151     dfs = []
152     for f in txt_files:
153         dfs.append(read_measurement_file(f))
154
155     merged = pd.concat(dfs, ignore_index=True)
156     merged["elapsed_s"] = np.arange(len(merged), dtype=float)
157     merged["elapsed_min"] = merged["elapsed_s"] / 60.0
158     merged["elapsed_h"] = merged["elapsed_s"] / 3600.0
159

```

```

160     return merged
161
162
163 # =====
164 # BINNING
165 # =====
166
167 def bin_counts(df: pd.DataFrame, bin_size_s: int):
168     """
169     Bin the 1-second count data into bins of length bin_size_s.
170
171     For each bin:
172         cps_bin = (sum of counts in bin) / (number of rows in bin)
173
174     This matches the manual:
175     "sum of counts in a time interval divided by the number of integrated rows"
176     """
177     if bin_size_s <= 0:
178         raise ValueError("bin_size_s must be positive.")
179
180     data = df.copy()
181
182     # Bin index based on row number, since each row = 1 second
183     data["bin_index"] = (np.arange(len(data)) // bin_size_s).astype(int)
184
185     grouped = data.groupby("bin_index", as_index=False).agg(
186         elapsed_s_start=("elapsed_s", "min"),
187         elapsed_s_end=("elapsed_s", "max"),
188         n_rows=("counts", "size"),
189         counts_sum=("counts", "sum"),
190         counts_mean=("counts", "mean"),
191     )
192
193     grouped["cps"] = grouped["counts_sum"] / grouped["n_rows"]
194     grouped["elapsed_s_center"] = 0.5 * (grouped["elapsed_s_start"] +
195 grouped["elapsed_s_end"])
196     grouped["elapsed_min_center"] = grouped["elapsed_s_center"] / 60.0
197     grouped["elapsed_h_center"] = grouped["elapsed_s_center"] / 3600.0
198
199     # Poisson uncertainty of mean cps in each bin:
200     # sigma = sqrt(total counts) / n_rows

```

```

200     grouped["sigma_cps"] = np.sqrt(grouped["counts_sum"]) / grouped["n_rows"]
201
202     return grouped
203
204
205 # =====
206 # SUMMARY STATISTICS
207 # =====
208
209 def measurement_summary(df: pd.DataFrame, binned_df: pd.DataFrame,
210     folder_name: str, bin_size_s: int):
211     counts = df["counts"].to_numpy(dtype=float)
212     n_seconds = len(counts)
213     total_counts = counts.sum()
214
215     mean_cps = total_counts / n_seconds
216     sigma_mean_cps = math.sqrt(total_counts) / n_seconds
217
218     std_1s = np.std(counts, ddof=1) if len(counts) > 1 else np.nan
219     std_binned = np.std(binned_df["cps"], ddof=1) if len(binned_df) > 1 else
220     np.nan
221
222     return {
223         "folder": folder_name,
224         "device": extract_device_number(folder_name),
225         "n_seconds": n_seconds,
226         "measurement_time_min": n_seconds / 60.0,
227         "measurement_time_h": n_seconds / 3600.0,
228         "bin_size_s": bin_size_s,
229         "n_bins": len(binned_df),
230         "total_counts": total_counts,
231         "mean_cps": mean_cps,
232         "sigma_mean_cps": sigma_mean_cps,
233         "std_1s_counts": std_1s,
234         "std_binned_cps": std_binned,
235     }
236
237 # =====
238 # PLOTTING
239 # =====

```

```

239
240 def plot_background(df: pd.DataFrame, binned_df: pd.DataFrame, folder_name:
    str, bin_size_s: int):
241     """
242     Plot raw 1-second counts and binned cps.
243     """
244     fig, ax = plt.subplots(figsize=(10, 5))
245
246     # raw 1-second counts
247     ax.plot(df["elapsed_min"], df["counts"], linewidth=0.7, alpha=0.6,
    label="Raw counts (1 s)")
248
249     # binned cps
250     ax.plot(
251         binned_df["elapsed_min_center"],
252         binned_df["cps"],
253         linewidth=2.0,
254         label=f"Binned cps ({bin_size_s} s bins)"
255     )
256
257     ax.set_title(folder_name)
258     ax.set_xlabel("Elapsed time (min)")
259     ax.set_ylabel("Counts / cps")
260     ax.legend()
261     ax.grid(True, alpha=0.3)
262
263     plt.tight_layout()
264
265     safe_name = re.sub(r'[^w\-\_\. ]', '_', folder_name).replace(" ", "_")
266     fig_path = OUTPUT_DIR / f"{safe_name}_background_plot.png"
267     plt.savefig(fig_path, dpi=200)
268
269     if SHOW_PLOTS:
270         plt.show()
271     else:
272         plt.close(fig)
273
274     return fig_path
275
276
277 # =====

```

```

278 # MAIN ANALYSIS
279 # =====
280
281 def analyze_background_folder(folder_name: str, bin_size_s: int):
282     folder = find_folder_by_exact_name(folder_name)
283
284     df = read_folder_measurement(folder)
285     binned_df = bin_counts(df, bin_size_s=bin_size_s)
286
287     summary = measurement_summary(
288         df=df,
289         binned_df=binned_df,
290         folder_name=folder_name,
291         bin_size_s=bin_size_s
292     )
293
294     fig_path = plot_background(df, binned_df, folder_name, bin_size_s)
295
296     if SAVE_BINNED_DATA:
297         safe_name = re.sub(r'[\w\-\_\. ]', '_', folder_name).replace(" ", "_")
298         binned_csv = OUTPUT_DIR / f"{safe_name}_binned.csv"
299         binned_df.to_csv(binned_csv, index=False)
300     else:
301         binned_csv = None
302
303     return summary, fig_path, binned_csv
304
305
306 if __name__ == "__main__":
307     print("Base directory :", BASE_DIR)
308     print("Data directory :", DATA_DIR)
309     print("Output directory:", OUTPUT_DIR)
310
311     all_summaries = []
312
313     for folder_name, bin_size_s in BACKGROUND_CONFIG.items():
314         print("\n" + "=" * 70)
315         print(f"Analyzing background folder: {folder_name}")
316         print(f"Chosen bin size: {bin_size_s} s")
317         print("=" * 70)
318

```

```

319     try:
320         summary, fig_path, binned_csv =
analyze_background_folder(folder_name, bin_size_s)
321
322         all_summaries.append(summary)
323
324         print(f"Device           : {summary['device']}")
325         print(f"Measurement time [min]:
{summary['measurement_time_min']:.2f}")
326         print(f"Measurement time [h]  :
{summary['measurement_time_h']:.3f}")
327         print(f"Number of seconds   : {summary['n_seconds']}")
328         print(f"Number of bins      : {summary['n_bins']}")
329         print(f"Mean cps           : {summary['mean_cps']:.6f} pm
{summary['sigma_mean_cps']:.6f}")
330         print(f"Std of 1 s counts    : {summary['std_1s_counts']:.6f}")
331         print(f"Std of binned cps    : {summary['std_binned_cps']:.6f}")
332         print(f"Plot saved to       : {fig_path}")
333         if binned_csv is not None:
334             print(f"Binned data saved to : {binned_csv}")
335
336     except Exception as e:
337         print(f"ERROR for folder '{folder_name}': {e}")
338
339     if all_summaries:
340         summary_df = pd.DataFrame(all_summaries)
341         summary_csv = OUTPUT_DIR / "background_summary.csv"
342         summary_df.to_csv(summary_csv, index=False)
343
344         print("\n" + "=" * 70)
345         print("FINAL BACKGROUND SUMMARY")
346         print("=" * 70)
347         print(summary_df.to_string(index=False))
348         print(f"\nSummary saved to: {summary_csv}")
349     else:
350         print("\nNo background results were produced.")
351
352
353
354 # =====
355 # PATHS

```

```

356 # =====
357
358 # Assumed folder structure:
359 # Datenauswertung/
360 # Python Code/
361 #     EnvironmentalRadioactivity.py
362 # Messdaten/
363
364 BASE_DIR = Path(__file__).resolve().parent.parent
365 DATA_DIR = BASE_DIR / "Messdaten"
366 OUTPUT_DIR = BASE_DIR / "calibration_analysis_output"
367 OUTPUT_DIR.mkdir(exist_ok=True)
368
369
370 # =====
371 # USER SETTINGS
372 # =====
373
374 # Folder names exactly as they appear in Messdaten
375 CALIBRATION_CONFIG = {
376     1: {
377         "background_folder": "Background first measurement 10 min (1)",
378         "calibration_folder": "calibration 1 hour (1)",
379         "bin_size_s": 300,    # 5 min bins, as recommended in the manual
380     },
381     2: {
382         "background_folder": "Background 2 hours (2)",
383         "calibration_folder": "calibration 1 hour (2)",
384         "bin_size_s": 300,
385     },
386     3: {
387         "background_folder": "Background 2 hours (3)",
388         "calibration_folder": "calibration 1 hour (3)",
389         "bin_size_s": 300,
390     },
391 }
392
393 SHOW_PLOTS = True
394 SAVE_BINNED_DATA = True
395
396

```

```

397 # =====
398 # PHYSICAL CONSTANTS FOR KCL CALIBRATION
399 # =====
400
401 KCL_MASS_G = 1.9
402 K40_ABUNDANCE = 0.000117      # 0.0117 %
403 K40_HALF_LIFE_Y = 1.248e9      # years
404 AVOGADRO = 6.02214076e23
405 MOLAR_MASS_KCL = 74.5513      # g/mol
406
407 # Keep total 40K activity for now
408 K40_BRANCHING_FACTOR = 1.0
409
410
411 # =====
412 # HELPERS
413 # =====
414
415 def extract_datetime_from_filename(filename: str):
416     match = re.search(r"(\d{4}_\d{2}_\d{2})\s+(\d{2}\.\d{2}\.\d{2})", filename)
417     if not match:
418         return None
419     return datetime.strptime(
420         f"{match.group(1)} {match.group(2)}",
421         "%Y_%m_%d %H.%M.%S"
422     )
423
424
425 def normalize_name(name: str):
426     return name.strip().lower()
427
428
429 def find_folder_by_exact_name(folder_name: str):
430     for folder in DATA_DIR.iterdir():
431         if folder.is_dir() and normalize_name(folder.name) ==
432         normalize_name(folder_name):
433             return folder
434     raise FileNotFoundError(f"Folder not found: {folder_name}")
435
436 def list_txt_files_sorted(folder: Path):

```

```

437     files = list(folder.glob("*.txt"))
438     return sorted(files, key=lambda f: extract_datetime_from_filename(f.name)
439                   or datetime.min)
440
441 # =====
442 # TXT READING
443 # =====
444
445 def read_measurement_file(file_path: Path):
446     """
447     Reads only the first two columns:
448     1) Date/Time
449     2) counts (1 sec)
450
451     All columns from column 3 onward are ignored.
452     """
453     encodings = ["utf-8", "latin1", "cp1252"]
454     last_error = None
455
456     for enc in encodings:
457         try:
458             df = pd.read_csv(
459                 file_path,
460                 sep="\t",
461                 encoding=enc,
462                 usecols=[0, 1]
463             )
464             break
465         except Exception as e:
466             last_error = e
467     else:
468         raise RuntimeError(f"Could not read {file_path.name}: {last_error}")
469
470     df.columns = ["Date/Time", "counts"]
471
472     out = pd.DataFrame()
473     out["datetime"] = pd.to_datetime(
474         df["Date/Time"],
475         format="%Y.%m.%d %H:%M:%S",
476         errors="coerce"

```

```

477     )
478     out["counts"] = pd.to_numeric(df["counts"], errors="coerce")
479     out["source_file"] = file_path.name
480     out["file_start_datetime"] = extract_datetime_from_filename(file_path.name)
481
482     out = out.dropna(subset=["counts"]).copy()
483     out["counts"] = out["counts"].astype(float)
484
485     return out
486
487
488 def read_folder_measurement(folder: Path):
489     txt_files = list_txt_files_sorted(folder)
490     if not txt_files:
491         raise FileNotFoundError(f"No txt files found in folder: {folder.name}")
492
493     dfs = []
494     for f in txt_files:
495         dfs.append(read_measurement_file(f))
496
497     merged = pd.concat(dfs, ignore_index=True)
498     merged["elapsed_s"] = np.arange(len(merged), dtype=float)
499     merged["elapsed_min"] = merged["elapsed_s"] / 60.0
500     merged["elapsed_h"] = merged["elapsed_s"] / 3600.0
501
502     return merged
503
504
505 # =====
506 # BINNING
507 # =====
508
509 def bin_counts(df: pd.DataFrame, bin_size_s: int):
510     if bin_size_s <= 0:
511         raise ValueError("bin_size_s must be positive.")
512
513     data = df.copy()
514     data["bin_index"] = (np.arange(len(data)) // bin_size_s).astype(int)
515
516     grouped = data.groupby("bin_index", as_index=False).agg(
517         elapsed_s_start=("elapsed_s", "min"),

```

```

518     elapsed_s_end=("elapsed_s", "max"),
519     n_rows=("counts", "size"),
520     counts_sum=("counts", "sum"),
521 )
522
523 grouped["cps"] = grouped["counts_sum"] / grouped["n_rows"]
524 grouped["elapsed_s_center"] = 0.5 * (grouped["elapsed_s_start"] +
grouped["elapsed_s_end"])
525 grouped["elapsed_min_center"] = grouped["elapsed_s_center"] / 60.0
526 grouped["elapsed_h_center"] = grouped["elapsed_s_center"] / 3600.0
527 grouped["sigma_cps"] = np.sqrt(grouped["counts_sum"]) / grouped["n_rows"]
528
529 return grouped
530
531
532 # =====
533 # STATISTICS / PHYSICS
534 # =====
535
536 def count_rate_stats(df: pd.DataFrame):
537     counts = df["counts"].to_numpy(dtype=float)
538     n_seconds = len(counts)
539
540     if n_seconds == 0:
541         raise ValueError("No data rows found.")
542
543     total_counts = counts.sum()
544     mean_cps = total_counts / n_seconds
545     sigma_mean_cps = math.sqrt(total_counts) / n_seconds
546
547     return {
548         "n_seconds": n_seconds,
549         "total_counts": total_counts,
550         "mean_cps": mean_cps,
551         "sigma_mean_cps": sigma_mean_cps,
552     }
553
554
555 def k40_activity_from_kcl_mass(mass_g: float):
556     """
557     Compute 40K activity in the KCl sample:

```

```
558     A = lambda * N
559     """
560     n_kcl_mol = mass_g / MOLAR_MASS_KCL
561     n_k_atoms = n_kcl_mol * AVOGADRO
562     n_k40_atoms = n_k_atoms * K40_ABUNDANCE
563
564     t_half_s = K40_HALF_LIFE_Y * 365.25 * 24 * 3600
565     decay_constant = math.log(2) / t_half_s
566
567     activity_bq = decay_constant * n_k40_atoms
568     activity_bq *= K40_BRANCHING_FACTOR
569
570     return activity_bq
571
572
573 def calibration_from_rates(activity_bq: float, raw_stats: dict, bg_stats:
574     dict):
575     raw_cps = raw_stats["mean_cps"]
576     sigma_raw = raw_stats["sigma_mean_cps"]
577
578     bg_cps = bg_stats["mean_cps"]
579     sigma_bg = bg_stats["sigma_mean_cps"]
580
581     net_cps = raw_cps - bg_cps
582     sigma_net = math.sqrt(sigma_raw**2 + sigma_bg**2)
583
584     if net_cps <= 0:
585         raise ValueError(f"Non-positive net count rate: {net_cps:.6f} cps")
586
587     k = activity_bq / net_cps
588     sigma_k = activity_bq * sigma_net / (net_cps**2)
589
590     efficiency = 1.0 / k
591     sigma_efficiency = sigma_k / (k**2)
592
593     return {
594         "raw_cps": raw_cps,
595         "sigma_raw": sigma_raw,
596         "bg_cps": bg_cps,
597         "sigma_bg": sigma_bg,
598         "net_cps": net_cps,
```

```

598     "sigma_net": sigma_net,
599     "k": k,
600     "sigma_k": sigma_k,
601     "efficiency": efficiency,
602     "sigma_efficiency": sigma_efficiency,
603 }
604
605
606 # =====
607 # PLOTTING
608 # =====
609
610 def plot_calibration(device: int, calib_df: pd.DataFrame, calib_binned:
611     pd.DataFrame):
612     fig, ax = plt.subplots(figsize=(10, 5))
613
614     ax.plot(
615         calib_df["elapsed_min"],
616         calib_df["counts"],
617         linewidth=0.7,
618         alpha=0.6,
619         label="Raw counts (1 s)"
620     )
621
622     bin_size_s = int(round(calib_binned["n_rows"].iloc[0]))
623     ax.plot(
624         calib_binned["elapsed_min_center"],
625         calib_binned["cps"],
626         linewidth=2.0,
627         label=f"Binned cps ({bin_size_s} s bins)"
628     )
629
630     ax.set_title(f"Calibration measurement detector {device}")
631     ax.set_xlabel("Elapsed time (min)")
632     ax.set_ylabel("Counts / cps")
633     ax.grid(True, alpha=0.3)
634     ax.legend()
635
636     plt.tight_layout()
637
638     fig_path = OUTPUT_DIR / f"calibration_detector{device}.png"

```

```
638     plt.savefig(fig_path, dpi=200)
639
640     if SHOW_PLOTS:
641         plt.show()
642     else:
643         plt.close(fig)
644
645     return fig_path
```

2. Calibration Efficiency.py

```

1 from pathlib import Path
2 import re
3 from datetime import datetime
4 import math
5 import traceback
6
7 import numpy as np
8 import pandas as pd
9 import matplotlib.pyplot as plt
10
11
12 # =====
13 # PATHS
14 # =====
15
16 # Assumed folder structure:
17 # Datenauswertung/
18 #   Python Code/
19 #       2. Calibration Efficiency.py
20 #   Messdaten/
21
22 BASE_DIR = Path(__file__).resolve().parent.parent
23 DATA_DIR = BASE_DIR / "Messdaten"
24 OUTPUT_DIR = BASE_DIR / "calibration_analysis_output"
25 OUTPUT_DIR.mkdir(exist_ok=True)
26
27
28 # =====
29 # USER SETTINGS
30 # =====
31
32 # We include 4 calibration cases:
33 # - detector 1 with 10 min background (main choice)
34 # - detector 1 with 5 h background (consistency check)
35 # - detector 2
36 # - detector 3
37 CALIBRATION_CONFIG = {
38     "detector1_10min_bg": {
39         "device": 1,
40         "background_folder": "Background first measurement 10 min (1)",

```

```

41     "calibration_folder": "Calibration 1 hour (1)",
42     "bin_size_s": 300,    # 5 min bins
43     "label": "Detector 1 (10 min background)",
44 },
45 "detector1_5h_bg": {
46     "device": 1,
47     "background_folder": "Background second measurement 5 hours (1)",
48     "calibration_folder": "Calibration 1 hour (1)",
49     "bin_size_s": 300,
50     "label": "Detector 1 (5 h background)",
51 },
52 "detector2": {
53     "device": 2,
54     "background_folder": "Background 2 hours (2)",
55     "calibration_folder": "Calibration 1 hour (2)",
56     "bin_size_s": 300,
57     "label": "Detector 2",
58 },
59 "detector3": {
60     "device": 3,
61     "background_folder": "Background 3 hours (3)",
62     "calibration_folder": "Calibration 1 hour (3)",
63     "bin_size_s": 300,
64     "label": "Detector 3",
65 },
66 }
67
68 # Set to False to avoid the script blocking on plt.show()
69 SHOW_PLOTS = True
70 SAVE_BINNED_DATA = True
71
72
73 # =====
74 # PHYSICAL CONSTANTS FOR KCl CALIBRATION
75 # =====
76
77 KCL_MASS_G = 1.9
78 K40_ABUNDANCE = 0.000117      # 0.0117 %
79 K40_HALF_LIFE_Y = 1.248e9      # years
80 AVOGADRO = 6.02214076e23
81 MOLAR_MASS_KCL = 74.5513      # g/mol

```

```

82
83 # Keep total 40K activity
84 K40_BRANCHING_FACTOR = 1.0
85
86
87 # =====
88 # HELPERS
89 # =====
90
91 def extract_datetime_from_filename(filename: str):
92     match = re.search(r"(\d{4}_\d{2}_\d{2})\s+(\d{2}\.\d{2}\.\d{2})", filename)
93     if not match:
94         return None
95     return datetime.strptime(
96         f"{match.group(1)} {match.group(2)}",
97         "%Y_%m_%d %H.%M.%S"
98     )
99
100
101 def normalize_name(name: str):
102     return name.strip().lower()
103
104
105 def find_folder_by_exact_name(folder_name: str):
106     for folder in DATA_DIR.iterdir():
107         if folder.is_dir() and normalize_name(folder.name) ==
108         normalize_name(folder_name):
109             return folder
110         raise FileNotFoundError(f"Folder not found: {folder_name}")
111
112
113 def list_txt_files_sorted(folder: Path):
114     files = list(folder.glob("*.txt"))
115     return sorted(files, key=lambda f: extract_datetime_from_filename(f.name)
116     or datetime.min)
117
118 # =====
119 # TXT READING
120 # =====

```

```
121 def read_measurement_file(file_path: Path):
122     """
123     Reads only the first two columns:
124     1) Date/Time
125     2) counts (1 sec)
126
127     All columns from column 3 onward are ignored.
128     """
129     encodings = ["utf-8", "latin1", "cp1252"]
130     last_error = None
131
132     for enc in encodings:
133         try:
134             df = pd.read_csv(
135                 file_path,
136                 sep="\t",
137                 encoding=enc,
138                 usecols=[0, 1]
139             )
140             break
141         except Exception as e:
142             last_error = e
143     else:
144         raise RuntimeError(f"Could not read {file_path.name}: {last_error}")
145
146     df.columns = ["Date/Time", "counts"]
147
148     out = pd.DataFrame()
149     out["datetime"] = pd.to_datetime(
150         df["Date/Time"],
151         format="%Y.%m.%d %H:%M:%S",
152         errors="coerce"
153     )
154     out["counts"] = pd.to_numeric(df["counts"], errors="coerce")
155     out["source_file"] = file_path.name
156     out["file_start_datetime"] = extract_datetime_from_filename(file_path.name)
157
158     out = out.dropna(subset=["counts"]).copy()
159     out["counts"] = out["counts"].astype(float)
160
161     return out
```

```

162
163
164 def read_folder_measurement(folder: Path):
165     txt_files = list_txt_files_sorted(folder)
166     if not txt_files:
167         raise FileNotFoundError(f"No txt files found in folder: {folder.name}")
168
169     dfs = []
170     for f in txt_files:
171         dfs.append(read_measurement_file(f))
172
173     merged = pd.concat(dfs, ignore_index=True)
174     merged["elapsed_s"] = np.arange(len(merged), dtype=float)
175     merged["elapsed_min"] = merged["elapsed_s"] / 60.0
176     merged["elapsed_h"] = merged["elapsed_s"] / 3600.0
177
178     return merged
179
180
181 # =====
182 # BINNING
183 # =====
184
185 def bin_counts(df: pd.DataFrame, bin_size_s: int):
186     if bin_size_s <= 0:
187         raise ValueError("bin_size_s must be positive.")
188
189     data = df.copy()
190     data["bin_index"] = (np.arange(len(data)) // bin_size_s).astype(int)
191
192     grouped = data.groupby("bin_index", as_index=False).agg(
193         elapsed_s_start=("elapsed_s", "min"),
194         elapsed_s_end=("elapsed_s", "max"),
195         n_rows=("counts", "size"),
196         counts_sum=("counts", "sum"),
197     )
198
199     grouped["cps"] = grouped["counts_sum"] / grouped["n_rows"]
200     grouped["elapsed_s_center"] = 0.5 * (grouped["elapsed_s_start"] +
201 grouped["elapsed_s_end"])
201     grouped["elapsed_min_center"] = grouped["elapsed_s_center"] / 60.0

```

```

202     grouped["elapsed_h_center"] = grouped["elapsed_s_center"] / 3600.0
203     grouped["sigma_cps"] = np.sqrt(grouped["counts_sum"]) / grouped["n_rows"]
204
205     return grouped
206
207
208     # =====
209     # STATISTICS / PHYSICS
210     # =====
211
212 def count_rate_stats(df: pd.DataFrame):
213     counts = df["counts"].to_numpy(dtype=float)
214     n_seconds = len(counts)
215
216     if n_seconds == 0:
217         raise ValueError("No data rows found.")
218
219     total_counts = counts.sum()
220     mean_cps = total_counts / n_seconds
221     sigma_mean_cps = math.sqrt(total_counts) / n_seconds
222
223     return {
224         "n_seconds": n_seconds,
225         "total_counts": total_counts,
226         "mean_cps": mean_cps,
227         "sigma_mean_cps": sigma_mean_cps,
228     }
229
230
231 def k40_activity_from_kcl_mass(mass_g: float):
232     """
233     Compute 40K activity in the KCl sample:
234     A = lambda * N
235     """
236     n_kcl_mol = mass_g / MOLAR_MASS_KCL
237     n_k_atoms = n_kcl_mol * AVOGADRO
238     n_k40_atoms = n_k_atoms * K40_ABUNDANCE
239
240     t_half_s = K40_HALF_LIFE_Y * 365.25 * 24 * 3600
241     decay_constant = math.log(2) / t_half_s
242

```

```
243     activity_bq = decay_constant * n_k40_atoms
244     activity_bq *= K40_BRANCHING_FACTOR
245
246     return activity_bq
247
248
249 def calibration_from_rates(activity_bq: float, raw_stats: dict, bg_stats:
    dict):
250     raw_cps = raw_stats["mean_cps"]
251     sigma_raw = raw_stats["sigma_mean_cps"]
252
253     bg_cps = bg_stats["mean_cps"]
254     sigma_bg = bg_stats["sigma_mean_cps"]
255
256     net_cps = raw_cps - bg_cps
257     sigma_net = math.sqrt(sigma_raw**2 + sigma_bg**2)
258
259     if net_cps <= 0:
260         return {
261             "raw_cps": raw_cps,
262             "sigma_raw": sigma_raw,
263             "bg_cps": bg_cps,
264             "sigma_bg": sigma_bg,
265             "net_cps": net_cps,
266             "sigma_net": sigma_net,
267             "k": np.nan,
268             "sigma_k": np.nan,
269             "efficiency": np.nan,
270             "sigma_efficiency": np.nan,
271         }
272
273     k = activity_bq / net_cps
274     sigma_k = activity_bq * sigma_net / (net_cps**2)
275
276     efficiency = 1.0 / k
277     sigma_efficiency = sigma_k / (k**2)
278
279     return {
280         "raw_cps": raw_cps,
281         "sigma_raw": sigma_raw,
282         "bg_cps": bg_cps,
```

```

283     "sigma_bg": sigma_bg,
284     "net_cps": net_cps,
285     "sigma_net": sigma_net,
286     "k": k,
287     "sigma_k": sigma_k,
288     "efficiency": efficiency,
289     "sigma_efficiency": sigma_efficiency,
290 }
291
292
293
294 # =====
295 # PLOTTING
296 # =====
297
298 def plot_calibration(case_name: str, label: str, calib_df: pd.DataFrame,
299                    calib_binned: pd.DataFrame):
300
301     ax.plot(
302         calib_df["elapsed_min"],
303         calib_df["counts"],
304         linewidth=0.7,
305         alpha=0.6,
306         label="Raw counts (1 s)"
307     )
308
309     bin_size_s = int(round(calib_binned["n_rows"].iloc[0]))
310     ax.plot(
311         calib_binned["elapsed_min_center"],
312         calib_binned["cps"],
313         linewidth=2.0,
314         label=f"Binned cps ({bin_size_s} s bins)"
315     )
316
317     ax.set_title(f"Calibration measurement: {label}")
318     ax.set_xlabel("Elapsed time (min)")
319     ax.set_ylabel("Counts / cps")
320     ax.grid(True, alpha=0.3)
321     ax.legend()
322

```

```

323     plt.tight_layout()
324
325     fig_path = OUTPUT_DIR / f"{case_name}.png"
326     plt.savefig(fig_path, dpi=200)
327
328     if SHOW_PLOTS:
329         plt.show()
330     else:
331         plt.close(fig)
332
333     return fig_path
334
335
336 # =====
337 # MAIN CALIBRATION ANALYSIS
338 # =====
339
340 def analyze_calibration_case(case_name: str, config: dict):
341     device = config["device"]
342     label = config["label"]
343
344     bg_folder = find_folder_by_exact_name(config["background_folder"])
345     cal_folder = find_folder_by_exact_name(config["calibration_folder"])
346     bin_size_s = config["bin_size_s"]
347
348     bg_df = read_folder_measurement(bg_folder)
349     cal_df = read_folder_measurement(cal_folder)
350
351     cal_binned = bin_counts(cal_df, bin_size_s=bin_size_s)
352
353     bg_stats = count_rate_stats(bg_df)
354     cal_stats = count_rate_stats(cal_df)
355
356     activity_bq = k40_activity_from_kcl_mass(KCL_MASS_G)
357     cal_results = calibration_from_rates(activity_bq, cal_stats, bg_stats)
358
359     fig_path = plot_calibration(case_name, label, cal_df, cal_binned)
360
361     if SAVE_BINNED_DATA:
362         binned_csv = OUTPUT_DIR / f"{case_name}_binned.csv"
363         cal_binned.to_csv(binned_csv, index=False)

```

```
364     else:
365         binned_csv = None
366
367     summary = {
368         "case_name": case_name,
369         "label": label,
370         "device": device,
371         "background_folder": config["background_folder"],
372         "calibration_folder": config["calibration_folder"],
373         "background_n_seconds": bg_stats["n_seconds"],
374         "background_mean_cps": cal_results["bg_cps"],
375         "background_sigma_cps": cal_results["sigma_bg"],
376         "calibration_n_seconds": cal_stats["n_seconds"],
377         "calibration_raw_mean_cps": cal_results["raw_cps"],
378         "calibration_raw_sigma_cps": cal_results["sigma_raw"],
379         "calibration_net_cps": cal_results["net_cps"],
380         "calibration_net_sigma_cps": cal_results["sigma_net"],
381         "kcl_activity_bq": activity_bq,
382         "k_factor": cal_results["k"],
383         "sigma_k_factor": cal_results["sigma_k"],
384         "efficiency": cal_results["efficiency"],
385         "sigma_efficiency": cal_results["sigma_efficiency"],
386         "bin_size_s": bin_size_s,
387     }
388
389     return summary, fig_path, binned_csv
390
391
392 if __name__ == "__main__":
393     print("Base directory :", BASE_DIR)
394     print("Data directory :", DATA_DIR)
395     print("Output directory:", OUTPUT_DIR)
396
397     all_results = []
398
399     for case_name, config in CALIBRATION_CONFIG.items():
400         print("\n" + "=" * 70)
401         print(f"Analyzing calibration case: {case_name}")
402         print("=" * 70)
403
404         try:
```

```

405     summary, fig_path, binned_csv =
analyze_calibration_case(case_name, config)
406     all_results.append(summary)
407
408     print(f"Label                : {summary['label']}")
409     print(f"Background folder     : {summary['background_folder']}")
410     print(f"Calibration folder     : {summary['calibration_folder']}")
411     print(f"Background mean cps      :
{summary['background_mean_cps']:.6f} pm
{summary['background_sigma_cps']:.6f}")
412     print(f"Calibration raw cps      :
{summary['calibration_raw_mean_cps']:.6f} pm
{summary['calibration_raw_sigma_cps']:.6f}")
413     print(f"Calibration net cps      :
{summary['calibration_net_cps']:.6f} pm
{summary['calibration_net_sigma_cps']:.6f}")
414     print(f"KCl activity [Bq]       : {summary['kcl_activity_bq']:.6f}")
415     print(f"k factor [Bq/cps]       : {summary['k_factor']:.6f} pm
{summary['sigma_k_factor']:.6f}")
416     print(f"Efficiency [cps/Bq]     : {summary['efficiency']:.6f} pm
{summary['sigma_efficiency']:.6f}")
417     print(f"Plot saved to           : {fig_path}")
418     if binned_csv is not None:
419         print(f"Binned data saved to : {binned_csv}")
420
421     except Exception as e:
422         print(f"ERROR for case {case_name}: {e}")
423         traceback.print_exc()
424
425 if all_results:
426     results_df = pd.DataFrame(all_results)
427     results_csv = OUTPUT_DIR / "calibration_summary_all_cases.csv"
428     results_df.to_csv(results_csv, index=False)
429
430     print("\n" + "=" * 70)
431     print("FINAL CALIBRATION SUMMARY")
432     print("=" * 70)
433     print(results_df.to_string(index=False))
434     print(f"\nSummary saved to: {results_csv}")
435 else:
436     print("\nNo calibration results were produced.")

```

3. Rn Environmental Samples Air and Water.py

```

1 from __future__ import annotations
2
3 import math
4 from pathlib import Path
5 from typing import Optional, Dict, Any, List
6
7 import numpy as np
8 import pandas as pd
9 import matplotlib.pyplot as plt
10 from scipy.optimize import curve_fit
11
12
13 # =====
14 # USER CONFIGURATION
15 # =====
16
17 BASE_DIR = Path(__file__).resolve().parents[1]
18 DATA_DIR = BASE_DIR / "Messdaten"
19 OUTPUT_DIR = BASE_DIR / "environmental_samples_analysis_output"
20
21 # Enter your real measured sample volumes here #####
22 WATER_VOLUME_L = 2.00    # manual: 2-3 L
23 AIR_VOLUME_M3 = 3.96    # manual: 25.0 m^3
24
25 # Plotting/fit convention:
26 # Negative background-subtracted activities are interpreted as compatible with
    background.
27 # The fit functions below use only activity_bq > 0.
28
29 # Dose model from manual
30 DOSE_EPS_R = 0.17        # nSv h^-1 per (Bq m^-3)
31 DOSE_EPS_D = 9.0         # nSv h^-1 per (Bq m^-3)
32 DOSE_F = 0.4
33 DOSE_OCCUPANCY_H_PER_YEAR = 2000.0
34
35 # Corrected calibration values from your latest calibration output
36 DETECTORS: Dict[int, Dict[str, float]] = {
37     2: {
38         "bg_cps": 0.540278,
39         "sigma_bg_cps": 0.008662,

```

```

40     "k_bq_per_cps": 11.207092,
41     "sigma_k_bq_per_cps": 0.126203,
42 },
43 3: {
44     "bg_cps": 0.539259,
45     "sigma_bg_cps": 0.007066,
46     "k_bq_per_cps": 11.957791,
47     "sigma_k_bq_per_cps": 0.138263,
48 },
49 }
50
51 ANALYSES: List[Dict[str, Any]] = [
52     {
53         "name": "water",
54         "label": "Environment Water 5 hours (2)",
55         "folder": "Environment Water 5 hours (2)",
56         "detector": 2,
57         "bin_s": 300,          # 5 min
58         "fit_tmin_min": 0.0,
59         "fit_tmax_min": 180.0, # adjust if needed
60         "volume_l": WATER_VOLUME_L,
61     },
62     {
63         "name": "air",
64         "label": "Environment Air 10 hours (3)",
65         "folder": "Environment Air 10 hours (3)",
66         "detector": 3,
67         "bin_s": 600,          # 10 min
68         "fit_tmin_min": 0.0,
69         "fit_tmax_min": 300.0, # adjust if needed
70         "volume_m3": AIR_VOLUME_M3,
71     },
72 ]
73
74 # Literature half-lives
75 T12_PB214_MIN = 26.9
76 T12_BI214_MIN = 19.7
77
78
79 # =====
80 # HELPER FUNCTIONS

```

```

81 # =====
82
83 def pm_str(value: float, sigma: Optional[float] = None, digits: int = 3) ->
    str:
84     if sigma is None or not np.isfinite(sigma):
85         return f"{value:.{digits}f}"
86     return f"{value:.{digits}f} pm {sigma:.{digits}f}"
87
88
89 def safe_mkdir(path: Path) -> None:
90     path.mkdir(parents=True, exist_ok=True)
91
92
93 def read_txt_file(path: Path) -> pd.DataFrame:
94     """
95     Read only the first two columns:
96     1) Date/Time
97     2) counts (1 sec)
98     Ignore all columns from the 3rd onward.
99
100     The Ranger text files are often saved in Windows ANSI encoding
101     (typically cp1252), not UTF-8.
102     """
103     last_error = None
104
105     for enc in ["utf-8", "cp1252", "latin-1"]:
106         try:
107             df = pd.read_csv(
108                 path,
109                 sep=r"\t+",
110                 engine="python",
111                 usecols=[0, 1],
112                 header=0,
113                 encoding=enc,
114             )
115             break
116         except UnicodeDecodeError as exc:
117             last_error = exc
118     else:
119         raise last_error
120

```

```

121     df.columns = ["DateTime", "counts"]
122
123     df["DateTime"] = pd.to_datetime(
124         df["DateTime"],
125         format="%Y.%m.%d %H:%M:%S",
126         errors="coerce"
127     )
128     df["counts"] = pd.to_numeric(df["counts"], errors="coerce")
129
130     df = df.dropna(subset=["DateTime", "counts"]).copy()
131     df["counts"] = df["counts"].astype(float)
132     return df
133
134
135 def read_measurement_folder(folder: Path) -> pd.DataFrame:
136     txt_files = sorted(folder.glob("*.txt"))
137     if not txt_files:
138         raise FileNotFoundError(f"No .txt files found in: {folder}")
139
140     frames = []
141     for txt_file in txt_files:
142         df = read_txt_file(txt_file)
143         df["source_file"] = txt_file.name
144         frames.append(df)
145
146     data = pd.concat(frames, ignore_index=True)
147     data =
148     data.sort_values("DateTime").drop_duplicates(subset=["DateTime"]).reset_index(drop=True)
149
150     t0 = data["DateTime"].iloc[0]
151     data["elapsed_s"] = (data["DateTime"] - t0).dt.total_seconds()
152     data["elapsed_min"] = data["elapsed_s"] / 60.0
153     data["elapsed_h"] = data["elapsed_s"] / 3600.0
154     return data
155
156 def bin_time_series(data: pd.DataFrame, bin_s: int) -> pd.DataFrame:
157     out = data.copy()
158     out["bin_index"] = (out["elapsed_s"] // bin_s).astype(int)
159
160     grouped = out.groupby("bin_index", as_index=False)

```

```

161
162     binned = grouped.agg(
163         t_start_s=("elapsed_s", "min"),
164         t_end_s=("elapsed_s", "max"),
165         n_rows=("counts", "size"),
166         counts_sum=("counts", "sum"),
167     )
168
169     binned["t_mid_s"] = 0.5 * (binned["t_start_s"] + binned["t_end_s"])
170     binned["t_mid_min"] = binned["t_mid_s"] / 60.0
171     binned["t_mid_h"] = binned["t_mid_s"] / 3600.0
172
173     # mean cps in each bin
174     binned["raw_cps"] = binned["counts_sum"] / binned["n_rows"]
175
176     # Poisson uncertainty on mean cps
177     binned["sigma_raw_cps"] = np.sqrt(np.clip(binned["counts_sum"], 0.0,
178         None)) / binned["n_rows"]
179
180     return binned
181
182 def apply_background_and_calibration(
183     binned: pd.DataFrame,
184     bg_cps: float,
185     sigma_bg_cps: float,
186     k_bq_per_cps: float,
187     sigma_k_bq_per_cps: float,
188 ) -> pd.DataFrame:
189     out = binned.copy()
190
191     out["bg_cps"] = bg_cps
192     out["sigma_bg_cps"] = sigma_bg_cps
193     out["net_cps"] = out["raw_cps"] - bg_cps
194     out["sigma_net_cps"] = np.sqrt(out["sigma_raw_cps"] ** 2 + sigma_bg_cps **
195         2)
196
197     out["activity_bq"] = out["net_cps"] * k_bq_per_cps
198     out["sigma_activity_bq"] = np.sqrt(
199         (k_bq_per_cps * out["sigma_net_cps"]) ** 2 +
200         (out["net_cps"] * sigma_k_bq_per_cps) ** 2

```

```

200     )
201
202     return out
203
204
205 def select_fit_window(
206     df: pd.DataFrame,
207     tmin_min: float = 0.0,
208     tmax_min: Optional[float] = None,
209 ) -> pd.DataFrame:
210     mask = df["t_mid_min"] >= tmin_min
211     if tmax_min is not None:
212         mask &= df["t_mid_min"] <= tmax_min
213     return df.loc[mask].copy()
214
215
216 # =====
217 # FIT MODELS
218 # =====
219
220 def model_decay_single(t_s: np.ndarray, a0: float, lamb: float) -> np.ndarray:
221     return a0 * np.exp(-lamb * t_s)
222
223
224 def model_decay_double(t_s: np.ndarray, a1: float, lamb1: float, a2: float,
225     lamb2: float) -> np.ndarray:
226     return a1 * np.exp(-lamb1 * t_s) + a2 * np.exp(-lamb2 * t_s)
227
228 def fit_single_decay(df: pd.DataFrame) -> Optional[Dict[str, float]]:
229     fit_df = df[(df["activity_bq"] > 0) & (df["sigma_activity_bq"] > 0)].copy()
230     if len(fit_df) < 4:
231         return None
232
233     t = fit_df["t_mid_s"].to_numpy(dtype=float)
234     y = fit_df["activity_bq"].to_numpy(dtype=float)
235     s = fit_df["sigma_activity_bq"].to_numpy(dtype=float)
236
237     p0 = [max(y[0], y.max()), np.log(2.0) / (30.0 * 60.0)]
238     bounds = ([0.0, 0.0], [np.inf, np.inf])
239

```

```

240     try:
241         popt, pcov = curve_fit(
242             model_decay_single,
243             t,
244             y,
245             p0=p0,
246             sigma=s,
247             absolute_sigma=True,
248             bounds=bounds,
249             maxfev=20000,
250         )
251     except Exception:
252         return None
253
254     perr = np.sqrt(np.diag(pcov))
255     a0, lamb = popt
256     sigma_a0, sigma_lamb = perr
257
258     t12_s = np.log(2.0) / lamb
259     sigma_t12_s = np.log(2.0) * sigma_lamb / (lamb ** 2)
260
261     y_fit = model_decay_single(t, *popt)
262     rss = float(np.sum((y - y_fit) ** 2))
263
264     return {
265         "a0_bq": a0,
266         "sigma_a0_bq": sigma_a0,
267         "lambda_per_s": lamb,
268         "sigma_lambda_per_s": sigma_lamb,
269         "t12_s": t12_s,
270         "sigma_t12_s": sigma_t12_s,
271         "rss": rss,
272     }
273
274
275 def fit_double_decay(df: pd.DataFrame) -> Optional[Dict[str, float]]:
276     fit_df = df[(df["activity_bq"] > 0) & (df["sigma_activity_bq"] > 0)].copy()
277     if len(fit_df) < 6:
278         return None
279
280     t = fit_df["t_mid_s"].to_numpy(dtype=float)

```

```

281 y = fit_df["activity_bq"].to_numpy(dtype=float)
282 s = fit_df["sigma_activity_bq"].to_numpy(dtype=float)
283
284 ymax = max(y.max(), 1e-9)
285 p0 = [
286     0.6 * ymax,
287     np.log(2.0) / (20.0 * 60.0),    # faster component
288     0.4 * ymax,
289     np.log(2.0) / (90.0 * 60.0),    # slower component
290 ]
291 bounds = ([0.0, 0.0, 0.0, 0.0], [np.inf, np.inf, np.inf, np.inf])
292
293 try:
294     popt, pcov = curve_fit(
295         model_decay_double,
296         t,
297         y,
298         p0=p0,
299         sigma=s,
300         absolute_sigma=True,
301         bounds=bounds,
302         maxfev=50000,
303     )
304 except Exception:
305     return None
306
307 perr = np.sqrt(np.diag(pcov))
308 a1, lamb1, a2, lamb2 = popt
309 sa1, sl1, sa2, sl2 = perr
310
311 # sort so component 1 is always the faster one
312 if lamb2 > lamb1:
313     a1, a2 = a2, a1
314     lamb1, lamb2 = lamb2, lamb1
315     sa1, sa2 = sa2, sa1
316     sl1, sl2 = sl2, sl1
317
318 t12_1_s = np.log(2.0) / lamb1
319 t12_2_s = np.log(2.0) / lamb2
320 sigma_t12_1_s = np.log(2.0) * sl1 / (lamb1 ** 2)
321 sigma_t12_2_s = np.log(2.0) * sl2 / (lamb2 ** 2)

```

```

322
323 y_fit = model_decay_double(t, a1, lamb1, a2, lamb2)
324 rss = float(np.sum((y - y_fit) ** 2))
325
326 return {
327     "a1_bq": a1,
328     "sigma_a1_bq": sa1,
329     "lambda1_per_s": lamb1,
330     "sigma_lambda1_per_s": sl1,
331     "a2_bq": a2,
332     "sigma_a2_bq": sa2,
333     "lambda2_per_s": lamb2,
334     "sigma_lambda2_per_s": sl2,
335     "t12_1_s": t12_1_s,
336     "sigma_t12_1_s": sigma_t12_1_s,
337     "t12_2_s": t12_2_s,
338     "sigma_t12_2_s": sigma_t12_2_s,
339     "rss": rss,
340 }
341
342
343 # =====
344 # PLOTTING
345 # =====
346
347 def plot_raw_and_binned(raw_df: pd.DataFrame, binned_df: pd.DataFrame, label:
348     str, outpath: Path) -> None:
349     plt.figure(figsize=(11, 6))
350     plt.plot(raw_df["elapsed_min"], raw_df["counts"], linewidth=0.8,
351         label="Raw counts (1 s)")
352     plt.plot(binned_df["t_mid_min"], binned_df["raw_cps"], linewidth=2.0,
353         label="Binned cps")
354     plt.xlabel("Elapsed time (min)")
355     plt.ylabel("Counts / cps")
356     plt.title(label)
357     plt.grid(True, alpha=0.3)
358     plt.legend()
359     plt.tight_layout()
360     plt.savefig(outpath, dpi=200)
361     plt.show()
362     plt.close()

```

```

360
361
362 def plot_activity_linear(
363     binned_df: pd.DataFrame,
364     label: str,
365     outpath: Path,
366     single_fit: Optional[Dict[str, float]] = None,
367     double_fit: Optional[Dict[str, float]] = None,
368 ) -> None:
369     t_min = binned_df["t_mid_min"].to_numpy(dtype=float)
370     t_s = binned_df["t_mid_s"].to_numpy(dtype=float)
371     y = binned_df["activity_bq"].to_numpy(dtype=float)
372     s = binned_df["sigma_activity_bq"].to_numpy(dtype=float)
373
374     positive_mask = y > 0
375     negative_mask = y <= 0
376
377     plt.figure(figsize=(11, 6))
378
379     # Positive, physically meaningful background-subtracted activities
380     if np.any(positive_mask):
381         plt.errorbar(
382             t_min[positive_mask],
383             y[positive_mask],
384             yerr=s[positive_mask],
385             fmt="o",
386             ms=4,
387             capsize=2,
388             label="Positive binned activity",
389         )
390
391     # Negative background-subtracted bins:
392     # not interpreted as negative activity, only as compatible with background
393     if np.any(negative_mask):
394         plt.errorbar(
395             t_min[negative_mask],
396             y[negative_mask],
397             yerr=s[negative_mask],
398             fmt="o",
399             ms=4,
400             capsize=2,

```

```

401         color="gray",
402         ecolor="gray",
403         alpha=0.6,
404         label="Compatible with background",
405     )
406
407     if single_fit is not None:
408         tfit = np.linspace(t_s.min(), t_s.max(), 500)
409         yfit = model_decay_single(tfit, single_fit["a0_bq"],
single_fit["lambda_per_s"])
410         plt.plot(tfit / 60.0, yfit, linewidth=2.0, label="Single-exp fit")
411
412     if double_fit is not None:
413         tfit = np.linspace(t_s.min(), t_s.max(), 500)
414         yfit = model_decay_double(
415             tfit,
416             double_fit["a1_bq"],
417             double_fit["lambda1_per_s"],
418             double_fit["a2_bq"],
419             double_fit["lambda2_per_s"],
420         )
421         plt.plot(tfit / 60.0, yfit, linewidth=2.0, label="Double-exp fit")
422
423     plt.axhline(0.0, color="black", linewidth=1.0, alpha=0.5)
424     plt.xlabel("Elapsed time (min)")
425     plt.ylabel("Background-corrected activity (Bq)")
426     plt.title(label)
427     plt.grid(True, alpha=0.3)
428     plt.legend()
429     plt.tight_layout()
430     plt.savefig(outpath, dpi=200)
431     plt.show()
432     plt.close()
433
434
435 def plot_activity_log(
436     binned_df: pd.DataFrame,
437     label: str,
438     outpath: Path,
439     single_fit: Optional[Dict[str, float]] = None,
440     double_fit: Optional[Dict[str, float]] = None,

```

```

441 ) -> None:
442     t_min = binned_df["t_mid_min"].to_numpy(dtype=float)
443     t_s = binned_df["t_mid_s"].to_numpy(dtype=float)
444     y = binned_df["activity_bq"].to_numpy(dtype=float)
445     s = binned_df["sigma_activity_bq"].to_numpy(dtype=float)
446
447     mask = y > 0
448     if not np.any(mask):
449         return
450
451     plt.figure(figsize=(11, 6))
452     plt.errorbar(t_min[mask], y[mask], yerr=s[mask], fmt="o", ms=4, capsize=2,
453                 label="Binned activity")
454
455     if single_fit is not None:
456         tfit = np.linspace(t_s.min(), t_s.max(), 500)
457         yfit = model_decay_single(tfit, single_fit["a0_bq"],
458                                 single_fit["lambda_per_s"])
459         yfit = np.clip(yfit, 1e-12, None)
460         plt.plot(tfit / 60.0, yfit, linewidth=2.0, label="Single-exp fit")
461
462     if double_fit is not None:
463         tfit = np.linspace(t_s.min(), t_s.max(), 500)
464         yfit = model_decay_double(
465             tfit,
466             double_fit["a1_bq"],
467             double_fit["lambda1_per_s"],
468             double_fit["a2_bq"],
469             double_fit["lambda2_per_s"],
470         )
471         yfit = np.clip(yfit, 1e-12, None)
472         plt.plot(tfit / 60.0, yfit, linewidth=2.0, label="Double-exp fit")
473
474     plt.yscale("log")
475     plt.xlabel("Elapsed time (min)")
476     plt.ylabel("Activity (Bq)")
477     plt.title(label + " (log scale)")
478     plt.grid(True, which="both", alpha=0.3)
479     plt.legend()
480     plt.tight_layout()
481     plt.savefig(outpath, dpi=200)

```

```

480     plt.show()
481     plt.close()
482
483
484     # =====
485     # ANALYSIS
486     # =====
487
488
489 def analyze_water(config: Dict[str, Any]) -> Dict[str, Any]:
490     folder = DATA_DIR / config["folder"]
491     detector = DETECTORS[config["detector"]]
492     outdir = OUTPUT_DIR / config["name"]
493     safe_mkdir(outdir)
494
495     raw_df = read_measurement_folder(folder)
496     binned = bin_time_series(raw_df, config["bin_s"])
497     binned = apply_background_and_calibration(
498         binned,
499         bg_cps=detector["bg_cps"],
500         sigma_bg_cps=detector["sigma_bg_cps"],
501         k_bq_per_cps=detector["k_bq_per_cps"],
502         sigma_k_bq_per_cps=detector["sigma_k_bq_per_cps"],
503     )
504
505     fit_df = select_fit_window(binned, config["fit_tmin_min"],
506                               config["fit_tmax_min"])
507     single_fit = fit_single_decay(fit_df)
508
509     plot_raw_and_binned(raw_df, binned, config["label"], outdir /
510                        "water_raw_binned.png")
511     plot_activity_linear(binned, config["label"], outdir /
512                        "water_activity_linear.png", single_fit=single_fit)
513
514     binned.to_csv(outdir / "water_binned.csv", index=False)
515
516     result: Dict[str, Any] = {
517         "name": "water",
518         "label": config["label"],
519         "detector": config["detector"],
520         "bin_s": config["bin_s"],

```

```

518     "n_raw_rows": len(raw_df),
519     "duration_h": raw_df["elapsed_h"].iloc[-1],
520     "single_fit_ok": single_fit is not None,
521 }
522
523 print("=" * 70)
524 print(f"Analyzing: {config['label']}")
525 print("=" * 70)
526 print(f"Folder           : {folder}")
527 print(f"Detector           : {config['detector']}")
528 print(f"Background cps      : {pm_str(detector['bg_cps'],
529 detector['sigma_bg_cps'], 6)}")
530 print(f"k factor [Bq/cps]   : {pm_str(detector['k_bq_per_cps'],
531 detector['sigma_k_bq_per_cps'], 6)}")
532 print(f"Rows read           : {len(raw_df)}")
533 print(f"Duration [h]         : {raw_df['elapsed_h'].iloc[-1]:.3f}")
534 print(f"Bin size [s]         : {config['bin_s']}")
535
536 if single_fit is not None:
537     t12_min = single_fit["t12_s"] / 60.0
538     sigma_t12_min = single_fit["sigma_t12_s"] / 60.0
539
540     result["a0_bq"] = single_fit["a0_bq"]
541     result["sigma_a0_bq"] = single_fit["sigma_a0_bq"]
542     result["t12_min"] = t12_min
543     result["sigma_t12_min"] = sigma_t12_min
544
545     print("Single exponential fit : OK")
546     print(f"A0 [Bq]           : {pm_str(single_fit['a0_bq'],
547 single_fit['sigma_a0_bq'], 3)}")
548     print(f"T1/2 [min]        : {pm_str(t12_min, sigma_t12_min, 3)}")
549
550     volume_l = config.get("volume_l", None)
551     if volume_l is not None and volume_l > 0:
552         c0_bq_per_l = single_fit["a0_bq"] / volume_l
553         sigma_c0_bq_per_l = single_fit["sigma_a0_bq"] / volume_l
554         result["c0_bq_per_l"] = c0_bq_per_l
555         result["sigma_c0_bq_per_l"] = sigma_c0_bq_per_l
556         print(f"C0 water [Bq/L]       : {pm_str(c0_bq_per_l,
557 sigma_c0_bq_per_l, 4)}")
558     else:

```

```

555         print("C0 water [Bq/L]          : Volume not set")
556     else:
557         print("Single exponential fit : FAILED")
558
559     print(f"Reference Pb-214 [min] : {T12_PB214_MIN:.1f}")
560     print(f"Reference Bi-214 [min] : {T12_BI214_MIN:.1f}")
561     print(f"Saved binned CSV       : {outdir / 'water_binned.csv'}")
562     print(f"Saved plots           : {outdir}")
563
564     return result
565
566
567 def analyze_air(config: Dict[str, Any]) -> Dict[str, Any]:
568     folder = DATA_DIR / config["folder"]
569     detector = DETECTORS[config["detector"]]
570     outdir = OUTPUT_DIR / config["name"]
571     safe_mkdir(outdir)
572
573     raw_df = read_measurement_folder(folder)
574     binned = bin_time_series(raw_df, config["bin_s"])
575     binned = apply_background_and_calibration(
576         binned,
577         bg_cps=detector["bg_cps"],
578         sigma_bg_cps=detector["sigma_bg_cps"],
579         k_bq_per_cps=detector["k_bq_per_cps"],
580         sigma_k_bq_per_cps=detector["sigma_k_bq_per_cps"],
581     )
582
583     fit_df = select_fit_window(binned, config["fit_tmin_min"],
584                               config["fit_tmax_min"])
585     single_fit = fit_single_decay(fit_df)
586     double_fit = fit_double_decay(fit_df)
587
588     plot_raw_and_binned(raw_df, binned, config["label"], outdir /
589                        "air_raw_binned.png")
590     plot_activity_linear(
591         binned,
592         config["label"],
593         outdir / "air_activity_linear.png",
594         single_fit=single_fit,
595         double_fit=double_fit,

```

```

594 )
595 plot_activity_log(
596     binned,
597     config["label"],
598     outdir / "air_activity_log.png",
599     single_fit=single_fit,
600     double_fit=double_fit,
601 )
602
603 binned.to_csv(outdir / "air_binned.csv", index=False)
604
605 result: Dict[str, Any] = {
606     "name": "air",
607     "label": config["label"],
608     "detector": config["detector"],
609     "bin_s": config["bin_s"],
610     "n_raw_rows": len(raw_df),
611     "duration_h": raw_df["elapsed_h"].iloc[-1],
612     "single_fit_ok": single_fit is not None,
613     "double_fit_ok": double_fit is not None,
614 }
615
616 print("=" * 70)
617 print(f"Analyzing: {config['label']}")
618 print("=" * 70)
619 print(f"Folder           : {folder}")
620 print(f"Detector           : {config['detector']}")
621 print(f"Background cps      : {pm_str(detector['bg_cps'],
622 detector['sigma_bg_cps'], 6)}")
623 print(f"k factor [Bq/cps]   : {pm_str(detector['k_bq_per_cps'],
624 detector['sigma_k_bq_per_cps'], 6)}")
625 print(f"Rows read           : {len(raw_df)}")
626 print(f"Duration [h]         : {raw_df['elapsed_h'].iloc[-1]:.3f}")
627 print(f"Bin size [s]         : {config['bin_s']}")
628
629 if single_fit is not None:
630     t12_min = single_fit["t12_s"] / 60.0
631     sigma_t12_min = single_fit["sigma_t12_s"] / 60.0
632
633     result["single_a0_bq"] = single_fit["a0_bq"]
634     result["single_sigma_a0_bq"] = single_fit["sigma_a0_bq"]

```

```

633     result["single_t12_min"] = t12_min
634     result["single_sigma_t12_min"] = sigma_t12_min
635
636     print("Single exponential fit : OK")
637     print(f"A0 [Bq]                : {pm_str(single_fit['a0_bq'],
single_fit['sigma_a0_bq'], 3)}")
638     print(f"T1/2 [min]            : {pm_str(t12_min, sigma_t12_min, 3)}")
639     else:
640         print("Single exponential fit : FAILED")
641
642     if double_fit is not None:
643         t12_fast_min = double_fit["t12_1_s"] / 60.0
644         sigma_t12_fast_min = double_fit["sigma_t12_1_s"] / 60.0
645         t12_slow_min = double_fit["t12_2_s"] / 60.0
646         sigma_t12_slow_min = double_fit["sigma_t12_2_s"] / 60.0
647
648         result["double_t12_fast_min"] = t12_fast_min
649         result["double_sigma_t12_fast_min"] = sigma_t12_fast_min
650         result["double_t12_slow_min"] = t12_slow_min
651         result["double_sigma_t12_slow_min"] = sigma_t12_slow_min
652
653         print("Double exponential fit : OK")
654         print(f"Fast T1/2 [min]        : {pm_str(t12_fast_min,
sigma_t12_fast_min, 3)}")
655         print(f"Slow T1/2 [min]       : {pm_str(t12_slow_min,
sigma_t12_slow_min, 3)}")
656     else:
657         print("Double exponential fit : FAILED")
658
659     volume_m3 = config.get("volume_m3", None)
660     if volume_m3 is not None and volume_m3 > 0 and single_fit is not None:
661         c0_bq_per_m3 = single_fit["a0_bq"] / volume_m3
662         sigma_c0_bq_per_m3 = single_fit["sigma_a0_bq"] / volume_m3
663
664         dose_nsv_per_year = c0_bq_per_m3 * (DOSE_EPS_R + DOSE_EPS_D * DOSE_F)
* DOSE_OCCUPANCY_H_PER_YEAR
665         sigma_dose_nsv_per_year = sigma_c0_bq_per_m3 * (DOSE_EPS_R +
DOSE_EPS_D * DOSE_F) * DOSE_OCCUPANCY_H_PER_YEAR
666
667         result["c0_bq_per_m3"] = c0_bq_per_m3
668         result["sigma_c0_bq_per_m3"] = sigma_c0_bq_per_m3

```

```

669     result["dose_nsv_per_year"] = dose_nsv_per_year
670     result["sigma_dose_nsv_per_year"] = sigma_dose_nsv_per_year
671     result["dose_msv_per_year"] = dose_nsv_per_year / 1e6
672     result["sigma_dose_msv_per_year"] = sigma_dose_nsv_per_year / 1e6
673
674     print(f"C0 air [Bq/m^3]           : {pm_str(c0_bq_per_m3,
sigma_c0_bq_per_m3, 4)}")
675     print(f"Dose [nSv/year]           : {pm_str(dose_nsv_per_year,
sigma_dose_nsv_per_year, 2)}")
676     print(f"Dose [mSv/year]           : {pm_str(dose_nsv_per_year / 1e6,
sigma_dose_nsv_per_year / 1e6, 6)}")
677     elif single_fit is not None:
678         print("C0 air [Bq/m^3]           : Volume not set")
679
680     print(f"Reference Pb-214 [min] : {T12_PB214_MIN:.1f}")
681     print(f"Reference Bi-214 [min] : {T12_BI214_MIN:.1f}")
682     print(f"Saved binned CSV       : {outdir / 'air_binned.csv'}")
683     print(f"Saved plots            : {outdir}")
684
685     return result
686
687
688 # =====
689 # MAIN
690 # =====
691
692 def main() -> None:
693     safe_mkdir(OUTPUT_DIR)
694
695     print(f"Base directory           : {BASE_DIR}")
696     print(f>Data directory            : {DATA_DIR}")
697     print(f"Output directory             : {OUTPUT_DIR}")
698     print("")
699
700     all_results: List[Dict[str, Any]] = []
701
702     for config in ANALYSES:
703         if config["name"] == "water":
704             result = analyze_water(config)
705         elif config["name"] == "air":
706             result = analyze_air(config)

```

```
707     else:
708         raise ValueError(f"Unknown analysis name: {config['name']}")
709
710     all_results.append(result)
711     print("")
712
713     summary_df = pd.DataFrame(all_results)
714     summary_path = OUTPUT_DIR / "environmental_samples_summary.csv"
715     summary_df.to_csv(summary_path, index=False)
716
717     print("=" * 70)
718     print("FINAL SUMMARY")
719     print("=" * 70)
720     print(summary_df.to_string(index=False))
721     print("")
722     print(f"Summary saved to      : {summary_path}")
723
724
725 if __name__ == "__main__":
726     main()
```

4. Ingrowth and Decay of Rn and Progeny.py

```

1 from __future__ import annotations
2
3 from pathlib import Path
4 from typing import Optional, Dict, Any, List
5
6 import numpy as np
7 import pandas as pd
8 import matplotlib.pyplot as plt
9 from scipy.optimize import curve_fit
10
11
12 # =====
13 # USER CONFIGURATION
14 # =====
15
16 BASE_DIR = Path(__file__).resolve().parents[1]
17 DATA_DIR = BASE_DIR / "Messdaten"
18 OUTPUT_DIR = BASE_DIR / "ingrowth_decay_analysis_output"
19
20 # Detector 1: use the final corrected calibration
21 DETECTOR_1 = {
22     "bg_cps": 0.502667,
23     "sigma_bg_cps": 0.005284,
24     "k_bq_per_cps": 11.503519,
25     "sigma_k_bq_per_cps": 0.127739,
26 }
27
28 # Folder names from your current structure
29 CONFIG = {
30     "ingrowth": {
31         "label": "Ingrowth and decay 4 hours (1)",
32         "folder": "Ingrowth and decay 4 hours (1)",
33         "bin_s": 300, # 5 min
34         "fit_tmin_min": 0.0,
35         "fit_tmax_min": 240.0,
36     },
37     "long_decay": {
38         "label": "Ingrowth and decay long 3 days (1)",
39         "folder": "Ingrowth and decay long 3 days (1)",
40         "bin_s": 3600, # 1 h

```

```

41     "fit_tmin_h": 0.0,
42     "fit_tmax_h": None,
43     "adsorption_time_h": 2.0, # from manual for decay measurement
44 },
45 }
46
47 # Literature values
48 T12_PB214_MIN = 26.9
49 T12_BI214_MIN = 19.7
50 T12_RN222_D = 3.8235
51 T12_RN222_H = T12_RN222_D * 24.0
52
53
54 # =====
55 # HELPERS
56 # =====
57
58 def safe_mkdir(path: Path) -> None:
59     path.mkdir(parents=True, exist_ok=True)
60
61
62 def pm_str(value: float, sigma: Optional[float] = None, digits: int = 3) ->
63     str:
64     if sigma is None or not np.isfinite(sigma):
65         return f"{value:.{digits}f}"
66     return f"{value:.{digits}f} pm {sigma:.{digits}f}"
67
68 def read_txt_file(path: Path) -> pd.DataFrame:
69     """
70     Read only the first two columns:
71         1) Date/Time
72         2) counts (1 sec)
73     Ignore all columns from the 3rd onward.
74     """
75     last_error = None
76
77     for enc in ["utf-8", "cp1252", "latin-1"]:
78         try:
79             df = pd.read_csv(
80                 path,

```

```

81         sep=r"\t+",
82         engine="python",
83         usecols=[0, 1],
84         header=0,
85         encoding=enc,
86     )
87     break
88     except UnicodeDecodeError as exc:
89         last_error = exc
90 else:
91     raise last_error
92
93 df.columns = ["DateTime", "counts"]
94
95 df["DateTime"] = pd.to_datetime(
96     df["DateTime"],
97     format="%Y.%m.%d %H:%M:%S",
98     errors="coerce"
99 )
100 df["counts"] = pd.to_numeric(df["counts"], errors="coerce")
101
102 df = df.dropna(subset=["DateTime", "counts"]).copy()
103 df["counts"] = df["counts"].astype(float)
104 return df
105
106
107 def read_measurement_folder(folder: Path) -> pd.DataFrame:
108     txt_files = sorted(folder.glob("*.txt"))
109     if not txt_files:
110         raise FileNotFoundError(f"No .txt files found in: {folder}")
111
112     frames = []
113     for txt_file in txt_files:
114         df = read_txt_file(txt_file)
115         df["source_file"] = txt_file.name
116         frames.append(df)
117
118     data = pd.concat(frames, ignore_index=True)
119     data =
120     data.sort_values("DateTime").drop_duplicates(subset=["DateTime"]).reset_index(drop=True)

```

```

121     t0 = data["DateTime"].iloc[0]
122     data["elapsed_s"] = (data["DateTime"] - t0).dt.total_seconds()
123     data["elapsed_min"] = data["elapsed_s"] / 60.0
124     data["elapsed_h"] = data["elapsed_s"] / 3600.0
125     return data
126
127
128 def bin_time_series(data: pd.DataFrame, bin_s: int) -> pd.DataFrame:
129     out = data.copy()
130     out["bin_index"] = (out["elapsed_s"] // bin_s).astype(int)
131
132     grouped = out.groupby("bin_index", as_index=False)
133
134     binned = grouped.agg(
135         t_start_s=("elapsed_s", "min"),
136         t_end_s=("elapsed_s", "max"),
137         n_rows=("counts", "size"),
138         counts_sum=("counts", "sum"),
139     )
140
141     binned["t_mid_s"] = 0.5 * (binned["t_start_s"] + binned["t_end_s"])
142     binned["t_mid_min"] = binned["t_mid_s"] / 60.0
143     binned["t_mid_h"] = binned["t_mid_s"] / 3600.0
144
145     binned["raw_cps"] = binned["counts_sum"] / binned["n_rows"]
146     binned["sigma_raw_cps"] = np.sqrt(np.clip(binned["counts_sum"], 0.0,
147         None)) / binned["n_rows"]
148
149     return binned
150
151 def apply_background_and_calibration(
152     binned: pd.DataFrame,
153     bg_cps: float,
154     sigma_bg_cps: float,
155     k_bq_per_cps: float,
156     sigma_k_bq_per_cps: float,
157 ) -> pd.DataFrame:
158     out = binned.copy()
159
160     out["bg_cps"] = bg_cps

```

```

161     out["sigma_bg_cps"] = sigma_bg_cps
162     out["net_cps"] = out["raw_cps"] - bg_cps
163     out["sigma_net_cps"] = np.sqrt(out["sigma_raw_cps"] ** 2 + sigma_bg_cps **
164     2)
165
166     out["activity_bq"] = out["net_cps"] * k_bq_per_cps
167     out["sigma_activity_bq"] = np.sqrt(
168         (k_bq_per_cps * out["sigma_net_cps"]) ** 2 +
169         (out["net_cps"] * sigma_k_bq_per_cps) ** 2
170     )
171     return out
172
173 # =====
174 # MODELS
175 # =====
176
177 def model_ingrowth_bateman(t_s: np.ndarray, a_inf: float, lamb_d: float) ->
178     np.ndarray:
179     """
180     Effective daughter ingrowth toward equilibrium:
181      $A_d(t) = A_{inf} * (1 - \exp(-\lambda_d t))$ 
182     """
183     return a_inf * (1.0 - np.exp(-lamb_d * t_s))
184
185 def model_decay_single(t_s: np.ndarray, a0: float, lamb: float) -> np.ndarray:
186     return a0 * np.exp(-lamb * t_s)
187
188 # =====
189 # FITS
190 # =====
191
192
193 def fit_ingrowth(df: pd.DataFrame) -> Optional[Dict[str, float]]:
194     fit_df = df[(df["activity_bq"] >= 0) & (df["sigma_activity_bq"] >
195     0)].copy()
196     if len(fit_df) < 4:
197         return None
198
199     t = fit_df["t_mid_s"].to_numpy(dtype=float)

```

```

199     y = fit_df["activity_bq"].to_numpy(dtype=float)
200     s = fit_df["sigma_activity_bq"].to_numpy(dtype=float)
201
202     p0 = [max(y.max(), 1e-6), np.log(2.0) / (26.9 * 60.0)]
203     bounds = ([0.0, 0.0], [np.inf, np.inf])
204
205     try:
206         popt, pcov = curve_fit(
207             model_ingrowth_bateman,
208             t,
209             y,
210             p0=p0,
211             sigma=s,
212             absolute_sigma=True,
213             bounds=bounds,
214             maxfev=20000,
215         )
216     except Exception:
217         return None
218
219     perr = np.sqrt(np.diag(pcov))
220     a_inf, lamb_d = popt
221     sigma_a_inf, sigma_lamb_d = perr
222
223     t12_s = np.log(2.0) / lamb_d
224     sigma_t12_s = np.log(2.0) * sigma_lamb_d / (lamb_d ** 2)
225
226     # time to 99% equilibrium and 7 half-lives
227     t_99_s = -np.log(0.01) / lamb_d
228     sigma_t_99_s = np.log(100.0) * sigma_lamb_d / (lamb_d ** 2)
229     t_7hl_s = 7.0 * t12_s
230     sigma_t_7hl_s = 7.0 * sigma_t12_s
231
232     y_fit = model_ingrowth_bateman(t, *popt)
233     rss = float(np.sum((y - y_fit) ** 2))
234
235     return {
236         "a_inf_bq": a_inf,
237         "sigma_a_inf_bq": sigma_a_inf,
238         "lambda_d_per_s": lamb_d,
239         "sigma_lambda_d_per_s": sigma_lamb_d,

```

```

240     "t12_s": t12_s,
241     "sigma_t12_s": sigma_t12_s,
242     "t_99_s": t_99_s,
243     "sigma_t_99_s": sigma_t_99_s,
244     "t_7hl_s": t_7hl_s,
245     "sigma_t_7hl_s": sigma_t_7hl_s,
246     "rss": rss,
247 }
248
249
250 def fit_long_decay(df: pd.DataFrame) -> Optional[Dict[str, float]]:
251     fit_df = df[(df["activity_bq"] > 0) & (df["sigma_activity_bq"] > 0)].copy()
252     if len(fit_df) < 4:
253         return None
254
255     t = fit_df["t_mid_s"].to_numpy(dtype=float)
256     y = fit_df["activity_bq"].to_numpy(dtype=float)
257     s = fit_df["sigma_activity_bq"].to_numpy(dtype=float)
258
259     p0 = [max(y[0], y.max()), np.log(2.0) / (3.8 * 24.0 * 3600.0)]
260     bounds = ([0.0, 0.0], [np.inf, np.inf])
261
262     try:
263         popt, pcov = curve_fit(
264             model_decay_single,
265             t,
266             y,
267             p0=p0,
268             sigma=s,
269             absolute_sigma=True,
270             bounds=bounds,
271             maxfev=20000,
272         )
273     except Exception:
274         return None
275
276     perr = np.sqrt(np.diag(pcov))
277     a0, lamb = popt
278     sigma_a0, sigma_lamb = perr
279
280     t12_s = np.log(2.0) / lamb

```

```

281     sigma_t12_s = np.log(2.0) * sigma_lamb / (lamb ** 2)
282
283     y_fit = model_decay_single(t, *popt)
284     rss = float(np.sum((y - y_fit) ** 2))
285
286     return {
287         "a0_bq": a0,
288         "sigma_a0_bq": sigma_a0,
289         "lambda_per_s": lamb,
290         "sigma_lambda_per_s": sigma_lamb,
291         "t12_s": t12_s,
292         "sigma_t12_s": sigma_t12_s,
293         "rss": rss,
294     }
295
296
297 # =====
298 # THEORY / DERIVED QUANTITIES
299 # =====
300
301 def secular_equilibrium_ratio_after_n_half_lives(n: float) -> float:
302     """
303     Daughter ingrowth fraction for  $A_d/A_{inf} = 1 - 2^{-n}$ 
304     """
305     return 1.0 - 2.0 ** (-n)
306
307
308 def estimate_ra226_activity_from_rn_ingrowth(a_rn0_bq: float,
309 adsorption_time_h: float) -> float:
310     """
311     Assume:
312     - secular equilibrium between 226Ra and daughters
313     - 100% adsorption efficiency of 222Rn on activated carbon
314     - activity accumulated during adsorption time t_ads:
315          $A_{Rn,ads} = A_{Ra} * (1 - \exp(-\lambda_{Rn} * t_{ads}))$ 
316     Therefore:
317          $A_{Ra} = A_{Rn,ads} / (1 - \exp(-\lambda_{Rn} * t_{ads}))$ 
318     """
319     lambda_rn_h = np.log(2.0) / T12_RN222_H
320     factor = 1.0 - np.exp(-lambda_rn_h * adsorption_time_h)
321     if factor <= 0:

```

```

321     return np.nan
322     return a_rn0_bq / factor
323
324
325 # =====
326 # PLOTTING
327 # =====
328
329 def plot_raw_and_binned(raw_df: pd.DataFrame, binned_df: pd.DataFrame, label:
    str, outpath: Path) -> None:
330     plt.figure(figsize=(11, 6))
331     plt.plot(raw_df["elapsed_min"], raw_df["counts"], linewidth=0.8,
        label="Raw counts (1 s)")
332     plt.plot(binned_df["t_mid_min"], binned_df["raw_cps"], linewidth=2.0,
        label="Binned cps")
333     plt.xlabel("Elapsed time (min)")
334     plt.ylabel("Counts / cps")
335     plt.title(label)
336     plt.grid(True, alpha=0.3)
337     plt.legend()
338     plt.tight_layout()
339     plt.savefig(outpath, dpi=200)
340     plt.show()
341     plt.close()
342
343
344 def plot_ingrowth_activity(
345     binned_df: pd.DataFrame,
346     fit_result: Optional[Dict[str, float]],
347     label: str,
348     outpath: Path,
349 ) -> None:
350     t_min = binned_df["t_mid_min"].to_numpy(dtype=float)
351     t_s = binned_df["t_mid_s"].to_numpy(dtype=float)
352     y = binned_df["activity_bq"].to_numpy(dtype=float)
353     s = binned_df["sigma_activity_bq"].to_numpy(dtype=float)
354
355     plt.figure(figsize=(11, 6))
356     plt.errorbar(t_min, y, yerr=s, fmt="o", ms=4, capsize=2, label="Binned
        activity")
357

```

```

358     if fit_result is not None:
359         tfit = np.linspace(t_s.min(), t_s.max(), 500)
360         yfit = model_ingrowth_bateman(tfit, fit_result["a_inf_bq"],
fit_result["lambda_d_per_s"])
361         plt.plot(tfit / 60.0, yfit, linewidth=2.0, label="Ingrowth fit")
362
363     plt.xlabel("Elapsed time (min)")
364     plt.ylabel("Activity (Bq)")
365     plt.title(label)
366     plt.grid(True, alpha=0.3)
367     plt.legend()
368     plt.tight_layout()
369     plt.savefig(outpath, dpi=200)
370     plt.show()
371     plt.close()
372
373
374 def plot_decay_activity(
375     binned_df: pd.DataFrame,
376     fit_result: Optional[Dict[str, float]],
377     label: str,
378     outpath_linear: Path,
379     outpath_log: Path,
380 ) -> None:
381     t_h = binned_df["t_mid_h"].to_numpy(dtype=float)
382     t_s = binned_df["t_mid_s"].to_numpy(dtype=float)
383     y = binned_df["activity_bq"].to_numpy(dtype=float)
384     s = binned_df["sigma_activity_bq"].to_numpy(dtype=float)
385
386     plt.figure(figsize=(11, 6))
387     plt.errorbar(t_h, y, yerr=s, fmt="o", ms=4, capsize=2, label="Binned
activity")
388
389     if fit_result is not None:
390         tfit = np.linspace(t_s.min(), t_s.max(), 500)
391         yfit = model_decay_single(tfit, fit_result["a0_bq"],
fit_result["lambda_per_s"])
392         plt.plot(tfit / 3600.0, yfit, linewidth=2.0, label="Single-exp fit")
393
394     plt.xlabel("Elapsed time (h)")
395     plt.ylabel("Activity (Bq)")

```

```

396     plt.title(label)
397     plt.grid(True, alpha=0.3)
398     plt.legend()
399     plt.tight_layout()
400     plt.savefig(outpath_linear, dpi=200)
401     plt.show()
402     plt.close()
403
404     mask = y > 0
405     plt.figure(figsize=(11, 6))
406     plt.errorbar(t_h[mask], y[mask], yerr=s[mask], fmt="o", ms=4, capsize=2,
407                  label="Binned activity")
408
409     if fit_result is not None:
410         tfit = np.linspace(t_s.min(), t_s.max(), 500)
411         yfit = model_decay_single(tfit, fit_result["a0_bq"],
412                                  fit_result["lambda_per_s"])
413         yfit = np.clip(yfit, 1e-12, None)
414         plt.plot(tfit / 3600.0, yfit, linewidth=2.0, label="Single-exp fit")
415
416     plt.yscale("log")
417     plt.xlabel("Elapsed time (h)")
418     plt.ylabel("Activity (Bq)")
419     plt.title(label + " (log scale)")
420     plt.grid(True, which="both", alpha=0.3)
421     plt.legend()
422     plt.tight_layout()
423     plt.savefig(outpath_log, dpi=200)
424     plt.show()
425     plt.close()
426
427 # =====
428 # ANALYSIS
429 # =====
430
431 def analyze_ingrowth() -> Dict[str, Any]:
432     cfg = CONFIG["ingrowth"]
433     folder = DATA_DIR / cfg["folder"]
434     outdir = OUTPUT_DIR / "ingrowth"
435     safe_mkdir(outdir)

```

```

435
436 raw_df = read_measurement_folder(folder)
437 binned = bin_time_series(raw_df, cfg["bin_s"])
438 binned = apply_background_and_calibration(
439     binned,
440     bg_cps=DETECTOR_1["bg_cps"],
441     sigma_bg_cps=DETECTOR_1["sigma_bg_cps"],
442     k_bq_per_cps=DETECTOR_1["k_bq_per_cps"],
443     sigma_k_bq_per_cps=DETECTOR_1["sigma_k_bq_per_cps"],
444 )
445
446 fit_df = binned[
447     (binned["t_mid_min"] >= cfg["fit_tmin_min"]) &
448     (binned["t_mid_min"] <= cfg["fit_tmax_min"])
449 ].copy()
450
451 fit_result = fit_ingrowth(fit_df)
452
453 plot_raw_and_binned(raw_df, binned, cfg["label"], outdir /
454 "ingrowth_raw_binned.png")
455 plot_ingrowth_activity(binned, fit_result, cfg["label"], outdir /
456 "ingrowth_activity_fit.png")
457 binned.to_csv(outdir / "ingrowth_binned.csv", index=False)
458
459 result: Dict[str, Any] = {
460     "section": "ingrowth",
461     "label": cfg["label"],
462     "bin_s": cfg["bin_s"],
463     "n_raw_rows": len(raw_df),
464     "duration_h": raw_df["elapsed_h"].iloc[-1],
465     "fit_ok": fit_result is not None,
466 }
467
468 print("=" * 70)
469 print(f"Analyzing: {cfg['label']}")
470 print("=" * 70)
471 print(f"Folder                : {folder}")
472 print(f"Background cps          : {pm_str(DETECTOR_1['bg_cps'],
473 DETECTOR_1['sigma_bg_cps'], 6)}")
474 print(f"k factor [Bq/cps]       : {pm_str(DETECTOR_1['k_bq_per_cps'],
475 DETECTOR_1['sigma_k_bq_per_cps'], 6)}")

```

```

472     print(f"Rows read          : {len(raw_df)}")
473     print(f"Duration [h]       : {raw_df['elapsed_h'].iloc[-1]:.3f}")
474     print(f"Bin size [s]       : {cfg['bin_s']}")
475
476     if fit_result is not None:
477         t12_min = fit_result["t12_s"] / 60.0
478         sigma_t12_min = fit_result["sigma_t12_s"] / 60.0
479         t99_h = fit_result["t_99_s"] / 3600.0
480         sigma_t99_h = fit_result["sigma_t_99_s"] / 3600.0
481         t7hl_h = fit_result["t_7hl_s"] / 3600.0
482         sigma_t7hl_h = fit_result["sigma_t_7hl_s"] / 3600.0
483
484         eq_fraction_7hl = secular_equilibrium_ratio_after_n_half_lives(7.0)
485
486         result.update({
487             "a_inf_bq": fit_result["a_inf_bq"],
488             "sigma_a_inf_bq": fit_result["sigma_a_inf_bq"],
489             "t12_min": t12_min,
490             "sigma_t12_min": sigma_t12_min,
491             "t99_h": t99_h,
492             "sigma_t99_h": sigma_t99_h,
493             "t7hl_h": t7hl_h,
494             "sigma_t7hl_h": sigma_t7hl_h,
495             "eq_fraction_7hl": eq_fraction_7hl,
496         })
497
498     print("Ingrowth fit          : OK")
499     print(f"A_inf [Bq]           : {pm_str(fit_result['a_inf_bq'],
500 fit_result['sigma_a_inf_bq'], 3)}")
501     print(f"Effective T1/2 [min]    : {pm_str(t12_min, sigma_t12_min,
502 3)}")
503     print(f"Reference Pb-214 [min]   : {T12_PB214_MIN:.1f}")
504     print(f"Reference Bi-214 [min]   : {T12_BI214_MIN:.1f}")
505     print(f"7 half-lives [h]        : {pm_str(t7hl_h, sigma_t7hl_h, 3)}")
506     print(f"99% equilibrium time [h] : {pm_str(t99_h, sigma_t99_h, 3)}")
507     print(f"Eq. fraction after 7 hl   : {eq_fraction_7hl:.6f}")
508
509     else:
510         print("Ingrowth fit          : FAILED")
511
512     print(f"Saved binned CSV          : {outdir / 'ingrowth_binned.csv'}")
513     print(f"Saved plots               : {outdir}")

```

```

511
512     return result
513
514
515 def analyze_long_decay() -> Dict[str, Any]:
516     cfg = CONFIG["long_decay"]
517     folder = DATA_DIR / cfg["folder"]
518     outdir = OUTPUT_DIR / "long_decay"
519     safe_mkdir(outdir)
520
521     raw_df = read_measurement_folder(folder)
522     binned = bin_time_series(raw_df, cfg["bin_s"])
523     binned = apply_background_and_calibration(
524         binned,
525         bg_cps=DETECTOR_1["bg_cps"],
526         sigma_bg_cps=DETECTOR_1["sigma_bg_cps"],
527         k_bq_per_cps=DETECTOR_1["k_bq_per_cps"],
528         sigma_k_bq_per_cps=DETECTOR_1["sigma_k_bq_per_cps"],
529     )
530
531     fit_df = binned[binned["t_mid_h"] >= cfg["fit_tmin_h"]].copy()
532     if cfg["fit_tmax_h"] is not None:
533         fit_df = fit_df[fit_df["t_mid_h"] <= cfg["fit_tmax_h"]].copy()
534
535     fit_result = fit_long_decay(fit_df)
536
537     plot_raw_and_binned(raw_df, binned, cfg["label"], outdir /
538         "long_decay_raw_binned.png")
539     plot_decay_activity(
540         binned,
541         fit_result,
542         cfg["label"],
543         outdir / "long_decay_activity_linear.png",
544         outdir / "long_decay_activity_log.png",
545     )
546     binned.to_csv(outdir / "long_decay_binned.csv", index=False)
547
548     result: Dict[str, Any] = {
549         "section": "long_decay",
550         "label": cfg["label"],
551         "bin_s": cfg["bin_s"],

```

```

551     "n_raw_rows": len(raw_df),
552     "duration_h": raw_df["elapsed_h"].iloc[-1],
553     "fit_ok": fit_result is not None,
554 }
555
556 print("=" * 70)
557 print(f"Analyzing: {cfg['label']}")
558 print("=" * 70)
559 print(f"Folder                : {folder}")
560 print(f"Background cps          : {pm_str(DETECTOR_1['bg_cps'],
DETECTOR_1['sigma_bg_cps'], 6)}")
561 print(f"k factor [Bq/cps]       : {pm_str(DETECTOR_1['k_bq_per_cps'],
DETECTOR_1['sigma_k_bq_per_cps'], 6)}")
562 print(f"Rows read              : {len(raw_df)}")
563 print(f"Duration [h]             : {raw_df['elapsed_h'].iloc[-1]:.3f}")
564 print(f"Bin size [s]            : {cfg['bin_s']}")
565
566 if fit_result is not None:
567     t12_h = fit_result["t12_s"] / 3600.0
568     sigma_t12_h = fit_result["sigma_t12_s"] / 3600.0
569
570     a_ra = estimate_ra226_activity_from_rn_ingrowth(
571         fit_result["a0_bq"],
572         cfg["adsorption_time_h"],
573     )
574     sigma_a_ra = estimate_ra226_activity_from_rn_ingrowth(
575         fit_result["sigma_a0_bq"],
576         cfg["adsorption_time_h"],
577     )
578
579     result.update({
580         "a0_bq": fit_result["a0_bq"],
581         "sigma_a0_bq": fit_result["sigma_a0_bq"],
582         "t12_h": t12_h,
583         "sigma_t12_h": sigma_t12_h,
584         "a_ra226_bq": a_ra,
585         "sigma_a_ra226_bq": sigma_a_ra,
586     })
587
588     print(f"Decay fit                : OK")

```

```

589     print(f"A0 [Bq]                                : {pm_str(fit_result['a0_bq'],
fit_result['sigma_a0_bq'], 3)}")
590     print(f"T1/2 [h]                                : {pm_str(t12_h, sigma_t12_h, 3)}")
591     print(f"Reference Rn-222 [h]                    : {T12_RN222_H:.3f}")
592     print(f"Estimated Ra-226 [Bq]                   : {pm_str(a_ra, sigma_a_ra, 3)}")
593     print(f"Adsorption time [h]                     : {cfg['adsorption_time_h']:.2f}")
594     else:
595         print("Decay fit                                : FAILED")
596
597     print("Note                                : Long measurement may be only partly
quantitative.")
598     print(f"Saved binned CSV                        : {outdir / 'long_decay_binned.csv'}")
599     print(f"Saved plots                             : {outdir}")
600
601     return result
602
603
604 # =====
605 # MAIN
606 # =====
607
608 def main() -> None:
609     safe_mkdir(OUTPUT_DIR)
610
611     print(f"Base directory                        : {BASE_DIR}")
612     print(f>Data directory                        : {DATA_DIR}")
613     print(f"Output directory                       : {OUTPUT_DIR}")
614     print("")
615
616     results: List[Dict[str, Any]] = []
617
618     results.append(analyze_ingrowth())
619     print("")
620     results.append(analyze_long_decay())
621     print("")
622
623     summary_df = pd.DataFrame(results)
624     summary_path = OUTPUT_DIR / "ingrowth_decay_summary.csv"
625     summary_df.to_csv(summary_path, index=False)
626
627     print("=" * 70)

```

```
628     print("FINAL SUMMARY")
629     print("=" * 70)
630     print(summary_df.to_string(index=False))
631     print("")
632     print(f"Summary saved to          : {summary_path}")
633
634
635 if __name__ == "__main__":
636     main()
```